Fort Norfolk Pier Rehabilitation and Expansion Project USACE, Norfolk District, Fort Norfolk, Virginia

APPENDIX A

Coastal Analysis and Wave Modeling



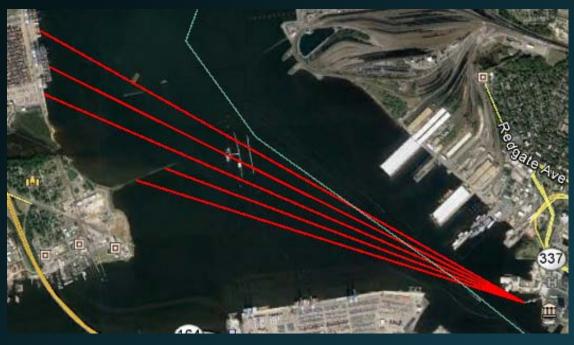
Coastal Analysis & Wave Modeling

McLaren Engineering Group

Content

- Limited Fetch Analysis
- Wave Model Description & Set Up
- Wave Modeling Results

Fetch Analysis



Fetch Analysis Summary Table

Fetch Direction	Hs (ft)	Tp (sec)
NW	5.03	3.44
SE	3.98	2.92

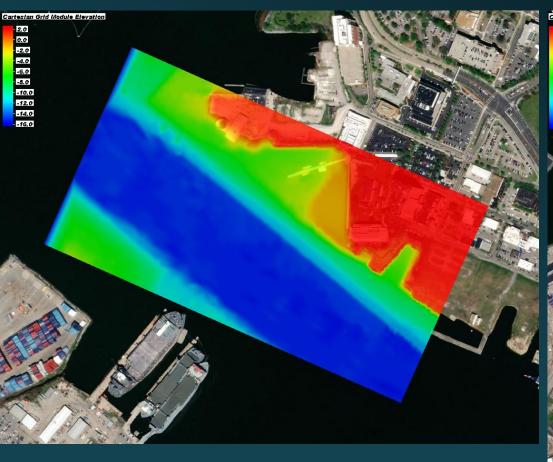


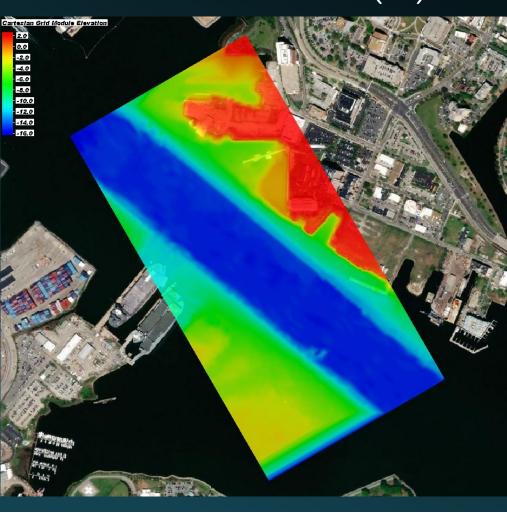
Wave Model - BOUSS-2D

- Simulating the propagation and transformation of waves in coastal regions and harbors
- Reflection/diffraction near structures
- Energy dissipation due to wave breaking and bottom friction
- Cross-spectral energy transfer due to nonlinear wave-wave interaction
- Breaking-induced longshore and rip currents
- Wave-current interaction
- Wave interaction with porous structures

NW Grid Elevation (m)

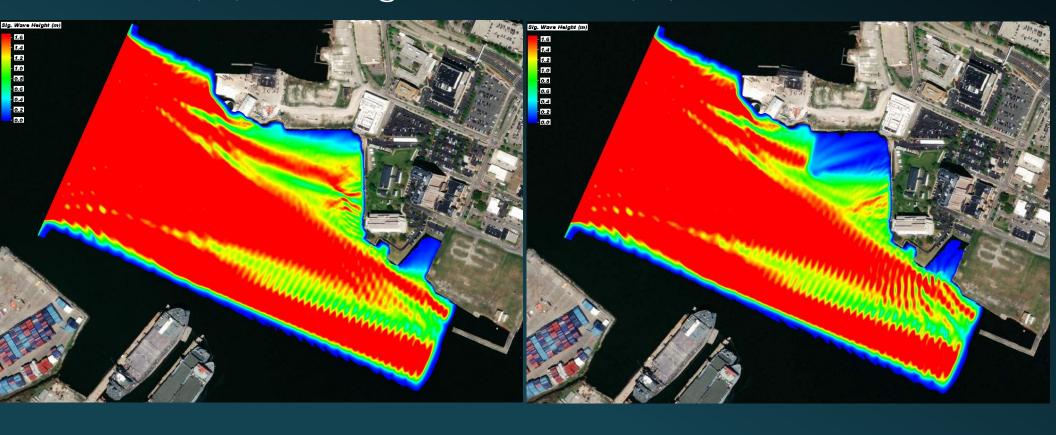
SE Grid Elevation (m)



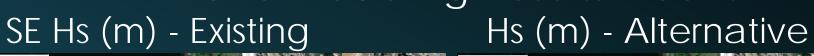


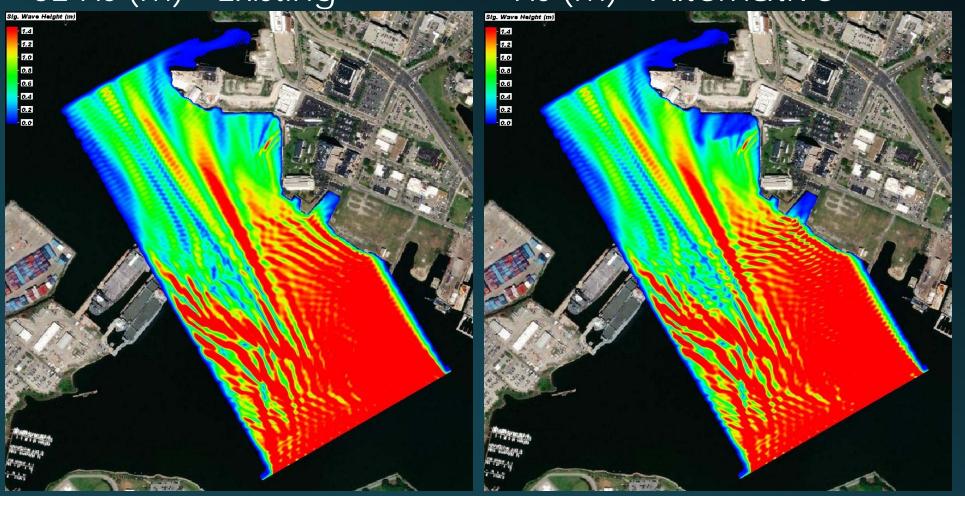
Alternative Design

Wave Modeling Results NW Hs (m) - Existing Hs (m) - Alternative



Wave Modeling Results - cont.





Wave Modeling Results - cont.



Significant Wave Height (m) Comparison @ Stations

	Station	1	2	3	4	5	6	7
Scenario		red	green	light blue	pink	dark blue	orange	brown
NW	Existing	1.50	0.99	1.02	0.64	1.94	0.17	0.30
Direction	Alternative	1.50	1.09	0.20	0.07	1.93	0.08	0.19
SE	Existing	0.50	0.64	0.59	0.28	1.46	0.70	0.26
Direction	Alternative	0.39	0.64	0.29	0.08	1.58	0.20	0.18



BOUSS-2D: A Boussinesq Wave Model for Coastal Regions and Harbors

Report 1
Theoretical Background and User's Manual
Okey George Nwogu and Zeki Demirbilek

September 2001

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BOUSS-2D: A Boussinesq Wave Model for Coastal Regions and Harbors

Report 1 Theoretical Background and User's Manual

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Report 1 of a series

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Preface

The work described herein was conducted by the U.S. Army Engineer Research and Development Center (ERDC), Coastal and Hydraulics Laboratory (CHL), under the Coastal Navigation Hydrodynamics Program work unit Waves in Entrance Channels. Overall program management was directed by the Hydraulic Design Section of Headquarters, U.S. Army Corps of Engineers (HQUSACE). Program Monitors were Messrs. Charles Chesnutt, Barry Holliday, and Mike Klosterman, HQUSACE. The Technical Director was Dr. William McAnally, CHL.

This study was conducted under the general supervision of Mr. Bruce A. Ebersole, Chief, Coastal Processes Branch (CPB), and Mr. Thomas W. Richardson, Acting Director, CHL. The report was prepared by Dr. Okey Nwogu, research scientist, Stevens Institute of Technology, and Dr. Zeki Demirbilek, research hydraulic engineer, Coastal Hydrodynamics Branch, CHL. Dr. Jane M. Smith (CPB) provided technical review of this report.

At the time of publication of this report, Dr. James R. Houston was Director of ERDC, and COL John W. Morris III, EN, was Commander and Executive Director.

1 Introduction

Background

An important component of most coastal and ocean engineering projects is an accurate assessment of the wave climate at the project site. Typical applications include determination of siltation rates inside entrance channels and harbor basins, determination of safe conditions for the loading/offloading of ships, optimization of harbor layouts for both wind-generated and long-period infragravity waves, design of structures such as breakwaters, and the evaluation of the impact of coastal structures on adjacent shorelines. Nearshore wave conditions are normally determined from deepwater conditions because long-term wave data are usually unavailable for most project sites. These offshore wave characteristics have to be transformed to the project site taking into account the effects of windwave generation, shoaling/refraction over seabed topography, energy dissipation due to wave breaking and bottom friction, wave reflection/diffraction near structures, nonlinear wave-wave interactions, and wave interaction with current fields.

A number of mathematical models have been developed to simulate the propagation and transformation of waves in coastal regions and harbors. The different models are based on different assumptions, which limit the types of problems to which they can be applied. Examples include spectral wind-wave models for wave propagation in open water where the processes of wind input, shoaling, and refraction are dominant; parabolic mild-slope equation models for wave propagation over large coastal areas when reflection is negligible; Helmholtz equation models for wave agitation and harbor resonance in water of constant depth; elliptic mild-slope models for wave agitation and harbor resonance in water of varying depth; and Boussinesq models for nonlinear wave refraction-diffraction in shallow water.

Numerical models available at the U.S. Army Corps of Engineers for predicting wave conditions in coastal regions and harbors include the spectral windwave model STWAVE (Smith, Sherlock, and Resio 2001) and the elliptic mild-slope model CGWAVE (Demirbilek and Panchang 1998). STWAVE is a windwave propagation model based on the wave action conservation equation. It is a phase-averaged model, i.e., it assumes that phase-averaged wave properties vary slowly over distances of the order of a wavelength. This allows the efficient computation of wave propagation over large open coastal areas. Due to the phase-averaging procedure, STWAVE cannot accurately resolve rapid variations that occur at subwavelength scales due to wave reflection/diffraction.

Chapter 1 Introduction 1

Phase resolving models based on either the mild-slope equation or Boussinesq-type equations are better suited for problems involving the reflection/diffraction of waves such as in coastal entrances and harbors. The mild-slope and Boussinesq equations are vertically integrated equations for wave propagation in the two-dimensional horizontal plane with different assumptions made for the variation of fluid motion over the water depth. The mild-slope equation derivation assumes a hyperbolic cosine variation of the velocity potential over depth, consistent with linear monochromatic waves in water of arbitrary depth, while the Boussinesq equation derivation assumes a quadratic profile, valid for shallow-water waves with wavelengths much longer than the water depth.

This report describes BOUSS-2D, a comprehensive numerical model based on a time-domain solution of Boussinesq-type equations. The classical form of the Boussinesq equations for wave propagation over water of variable depth was derived by Peregrine (1967). The equations were restricted to relatively shallowwater depths, i.e., the water depth, h, had to be less than one-fifth of the wavelength, L, in order to keep errors in the phase velocity to less than 5 percent. Nwogu (1993) extended the range of applicability of Boussinesq-type equations to deeper water by recasting the equations in terms of the velocity at an arbitrary distance z_{α} from the still-water level, instead of the depth-averaged velocity. The elevation of the velocity variable z_{α} becomes a free parameter, which is chosen to optimize the linear dispersion characteristics of the equations. The optimized form of the equations has errors of less than 2 percent in the phase velocity from shallow-water depths up to the deepwater limit (h/L = 0.5).

Despite the improvement in the frequency dispersion characteristics, Nwogu's (1993) equations are based on the assumption that the wave heights were much smaller than the water depth. This limits the ability of the equations to describe highly nonlinear waves in shallow water and led Wei et al. (1995) to derive a fully nonlinear form of the equations. The fully nonlinear equations are particularly useful for simulating highly asymmetric waves in shallow water, wave-induced currents, wave setup close to the shoreline, and wave-current interaction.

As ocean waves approach the shoreline, they steepen and ultimately break. The turbulence and currents generated by breaking waves are important driving mechanisms for the transport of sediments and pollutants. Nwogu (1996) extended the fully nonlinear form of the Boussinesq equations to the surf zone, by coupling the mass and momentum equations with a one-equation model for the temporal and spatial evolution of the turbulent kinetic energy produced by wave breaking. The equations have also been modified to include the effects of bottom friction and flow through porous structures. The modified equations can simulate most of the hydrodynamic phenomena of interest in coastal regions and harbor basins including:

- a. Shoaling.
- b. Refraction.
- c. Diffraction.

- d. Full/partial reflection and transmission.
- e. Bottom friction.
- f. Nonlinear wave-wave interactions.
- g. Wave breaking and runup.
- h. Wave-induced currents.
- Wave-current interaction.

A time domain, finite-difference method is used to solve the Boussinesq equations. The area of interest is discretized as a rectangular grid with the water-surface elevation and horizontal velocities defined at the grid nodes in a staggered manner. Time-histories of the velocities and fluxes corresponding to incident storm conditions are specified along external or internal wave generation boundaries. The wave conditions may be periodic or nonperiodic, unidirectional or multidirectional. Waves propagating out of the computational domain are absorbed in damping layers placed around the perimeter of the numerical basin. Porosity layers can be placed inside the computational domain to simulate the reflection and transmission characteristics of structures such as breakwaters.

Purpose

This report describes BOUSS-2D, a comprehensive numerical model for simulating the propagation and transformation of waves in coastal regions and harbors based on a time-domain solution of Boussinesq-type equations. An overview of the theoretical background behind the model is described in Chapter 2. The numerical scheme used to solve the equations is described in Chapter 3. The steps involved in setting up and running the model are described in Chapter 4. A number of analytical, laboratory, and field test cases have also been used to validate the model in Chapter 5. The different test cases were selected in Chapter 5 to evaluate the ability of the model to deal with individual wave transformation processes such as refraction, diffraction, wave breaking, etc., as well as the combination of processes that occur in practical engineering problems. Chapter 6 provides a summary and conclusions.

Chapter 1 Introduction 3

2 Theoretical Background

Governing Equations

BOUSS-2D is based on Boussinesq-type equations derived by Nwogu (1993, 1996). The equations are depth-integrated equations for the conservation of mass and momentum for nonlinear waves propagating in shallow and intermediate water depths. They can be considered to be a perturbation from the shallow-water equations, which are often used to simulate tidal flows in coastal regions. For short-period waves, the horizontal velocities are no longer uniform over depth and the pressure is nonhydrostatic. The vertical profile of the flow field is obtained by expanding the velocity potential, Φ , as a Taylor series about an arbitrary elevation, z_{α} , in the water column. For waves with length, L, much longer than the water depth, L, the series is truncated at second order resulting in a quadratic variation of the velocity potential over depth:

$$\Phi(x,z,t) = \phi_{\alpha} + \mu^{2}(z_{\alpha} - z) \left[\nabla \phi_{\alpha} \cdot \nabla h \right] + \frac{\mu^{2}}{2} \left[\left(z_{\alpha} + h \right)^{2} - (z + h)^{2} \right] \nabla^{2} \phi_{\alpha} + O(\mu^{4})$$
(1)

where $\phi_{\alpha} = \Phi(x, z_{\alpha}, t)$, $\nabla = (\partial/\partial x, \partial/\partial y)$, and $\mu = h/L$ is a measure of frequency dispersion. The horizontal and vertical velocities are obtained from the velocity potential as:

$$u(x,z,t) = \nabla \Phi = u_{\alpha} + (z_{\alpha} - z) \left[\nabla (u_{\alpha} \cdot \nabla h) + (\nabla \cdot u_{\alpha}) \nabla h \right] + \frac{1}{2} \left[\left(z_{\alpha} + h \right)^{2} - \left(z + h \right)^{2} \right] \nabla (\nabla \cdot u_{\alpha})$$
 (2)

$$w(x,z,t) = \frac{\partial \Phi}{\partial z} = -[\mathbf{u}_{\alpha} \cdot \nabla h + (z+h)\nabla \cdot \mathbf{u}_{\alpha}]$$
 (3)

where $u_{\alpha} = \nabla \Phi|_{z_{\alpha}}$ is the horizontal velocity at $z = z_{\alpha}$. Given a vertical profile for the flow field, the continuity and Euler (momentum) equations can be integrated over depth, reducing the three-dimensional problem to two dimensions. For weakly nonlinear waves with height, H, much smaller than the water depth, h, the vertically integrated equations are written in terms of the water-surface elevation $\eta(x,t)$ and velocity $u_{\alpha}(x,t)$ as (Nwogu 1993):

$$\eta_t + \nabla \cdot \boldsymbol{u}_f = 0 \tag{4}$$

$$u_{\alpha,t} + g\nabla \eta + (u_{\alpha} \cdot \nabla)u_{\alpha} + z_{\alpha} \Big[\nabla (u_{\alpha,t} \cdot \nabla h) + (\nabla \cdot u_{\alpha,t})\nabla h \Big]$$

$$+ \frac{1}{2} \Big[(z_{\alpha} + h)^{2} - h^{2} \Big] \nabla (\nabla \cdot u_{\alpha,t}) = 0$$
(5)

where g is the gravitational acceleration and u_f is the volume flux density given by:

$$u_{f} = \int_{-h}^{\eta} u \, dz = (h + \eta) u_{\alpha} + h \left(z_{\alpha} + \frac{h}{2} \right) \left[\nabla (u_{\alpha} \cdot \nabla h) + (\nabla \cdot u_{\alpha}) \nabla h \right] + h \left[\frac{\left(z_{\alpha} + h \right)^{2}}{2} - \frac{h^{2}}{6} \right] \nabla (\nabla \cdot u_{\alpha})$$

$$(6)$$

The depth-integrated equations are able to describe the propagation and transformation of irregular multidirectional waves over water of variable depth. The elevation of the velocity variable z_{α} is a free parameter and is chosen to minimize the differences between the linear dispersion characteristics of the model and the exact dispersion relation for small amplitude waves. The optimal value, $z_{\alpha} = -0.535h$, is close to middepth.

For steep near-breaking waves in shallow water, the wave height becomes of the order of the water depth and the weakly nonlinear assumption made in deriving Equations 4 and 5 is no longer valid. Wei et al. (1995) derived a fully nonlinear form of the equations from the dynamic free surface boundary condition by retaining all nonlinear terms, up to the order of truncation of the dispersive terms. Nwogu (1996) derived a more compact form of the equations by expressing some of the nonlinear terms as a function of the velocity at the free surface, u_{η} , instead of u_{α} . Additional changes have also been made to the equations to allow for weakly rotational flows in the horizontal plane and ensure that z_{α} remains in the water column for steep waves near the shoreline and during the wave runup process. The revised form of the fully nonlinear equations can be written as:

$$\eta_t + \nabla \cdot \boldsymbol{u}_f = 0 \tag{7}$$

$$u_{\alpha,t} + g\nabla\eta + (u_{\eta} \cdot \nabla)u_{\eta} + w_{\eta}\nabla w_{\eta} + (z_{\alpha} - \eta)\Big[\nabla(u_{\alpha,t} \cdot \nabla h) + (\nabla \cdot u_{\alpha,t})\nabla h\Big]$$

$$+ \frac{1}{2}\Big[(z_{\alpha} + h)^{2} - (h + \eta)^{2}\Big]\nabla(\nabla \cdot u_{\alpha,t})$$

$$- \Big[(u_{\alpha,t} \cdot \nabla h) + (h + \eta)\nabla \cdot u_{\alpha,t}\Big]\nabla\eta$$

$$+ \Big[\nabla(u_{\alpha,t} \cdot \nabla h) + (\nabla \cdot u_{\alpha,t})\nabla h + (z_{\alpha} + h)\nabla(\nabla \cdot u_{\alpha})\Big]z_{\alpha,t} = 0$$
(8)

where z_{α} is now a function of time and is given by $z_{\alpha}+h=0.465(h+\eta)$. The volume flux density u_f is given by:

$$\mathbf{u}_{f} = (h+\eta) \left\{ \mathbf{u}_{\alpha} + \left[(z_{\alpha} + h) - \frac{(h+\eta)}{2} \right] \left[\nabla (\mathbf{u}_{\alpha} \cdot \nabla h) + (\nabla \cdot \mathbf{u}_{\alpha}) \nabla h \right] + \left[\frac{(z_{\alpha} + h)^{2}}{2} - \frac{(h+\eta)^{2}}{6} \right] \nabla (\nabla \cdot \mathbf{u}_{\alpha}) \right\}$$
(9)

The fully nonlinear equations are able to implicitly model the effects of wavecurrent interaction. Currents can either be introduced through the boundaries or by explicitly specifying a current field, U.

Linear Dispersion Properties

The linear dispersion relation of the Boussinesq model that relates the wavelength, L, to the wave period, T, is given by Nwogu (1993) as:

$$C^{2} = \frac{L^{2}}{T^{2}} = \left[\frac{1 - (\alpha + 1/3)(kh)^{2}}{1 - \alpha(kh)^{2}} \right]$$
 (10)

where C is the phase speed, $k = 2\pi/L$ is the wave number, and $\alpha = [(z_{\alpha}+h)^2/h^2 - 1]/2$. Depending on the elevation of the velocity variable or the value of α , different dispersion relations are obtained. If the velocity at the seabed $(z_{\alpha} = -h)$ is used, $\alpha = -1/2$. Alternatively, if the velocity at the still-water level $(z_{\alpha} = 0)$ is used, $\alpha = 0$. The dispersion relation of the classical form of the Boussinesq equations which uses the depth-averaged velocity as the velocity variable corresponds to $\alpha = -1/3$. Witting (1984) obtained the value $\alpha = -2/5$ from the Padé (2,2) approximant of tanh kh.

The phase speeds for different values of α , normalized with respect to the linear theory phase speed are plotted as a function of relative depth in Figure 1. The relative depth is defined as the ratio of the water depth, h, to the equivalent deepwater wavelength $L_o = gT^2/2\pi$. The deepwater depth limit corresponds to h/L = 0.5. The different dispersion equations are all equivalent in relatively shallow water (h/L < 0.02), but gradually diverge from the exact solution with increasing depth. An optimal depth $z_{\alpha} = -0.535h$ gives errors of less than 2 percent in the phase velocity from shallow-water depths up to the deepwater limit.

Nonlinear Properties

In an irregular sea state, different frequency components interact to generate forced waves at the sum and difference frequencies of the primary waves because of the nonlinear nature of the boundary condition at the free surface. Consider a

(1994) derived similar expressions for the weakly nonlinear form of the Boussinesq equations:

$$G_{\pm}(\omega_{1}, \omega_{2}) = \frac{\omega_{1}\omega_{2}(k_{\pm}h)^{2}\cos\Delta\theta[1 - (\alpha + 1/3)(k_{\pm}h)^{2}]}{2\lambda k_{1}^{2}k_{2}^{2}h^{3}} + \frac{\omega_{\pm}[1 - \alpha(k_{\pm}h)^{2}][\omega_{1}k_{2}^{2}h(k_{1}h \pm k_{2}h\cos\Delta\theta) + \omega_{2}k_{1}^{2}h(k_{1}h\cos\Delta\theta \pm k_{2}h)]}{2\lambda k_{1}^{2}k_{2}^{2}h^{3}}$$
(13)

where
$$Dq = q1 \pm q2$$
, $k \pm = |k1 \pm k2|$, $k' = k[1 - (\alpha + 1/3) (kh)2]$, and $\lambda = \omega_+^2 [1 - \alpha (k_+ h)^2] - g k_+^2 h [1 - (\alpha + 1/3) (k_+ h)^2]$ (14)

Figure 2 shows a comparison of the quadratic transfer function of the weakly nonlinear Boussinesq model with that of second-order Stokes theory for unidirectional waves where the wave group period is 10 times the average of the individual wave periods, i.e., $\omega_- = (\omega_1 + \omega_2)/20$. The weakly nonlinear Boussinesq model underestimates the magnitude of the setdown wave and second harmonic at the deepwater depth limit by 65 percent and 45 percent respectively. Hence, it cannot accurately simulate nonlinear effects in deep water. To reasonably simulate nonlinear effects, the weakly nonlinear model should be restricted to the range 0 < h/L < 0.3.

Simulation of Wave Breaking

The turbulent and highly rotational flow field under breaking waves is extremely complex and difficult to model even with the Reynolds-averaged form of the Navier-Stokes equations (e.g., Lin and Liu 1998; Bradford 2000). In BOUSS-2D, we do not attempt to model details of the turbulent motion, but rather, simulate the effect of breaking-induced turbulence on the flow field. We have tried to develop a generic model that can be applied to regular or irregular waves, unidirectional or multidirectional waves, and simple or complex bottom topography without having to recalibrate the model each time. The key assumptions made in developing the model are (see Nwogu 1996):

- a. The breaking process is assumed to be "spilling."
- b. Turbulence is produced in the near-surface region when the horizontal velocity at the free surface, u_n , exceeds the phase velocity, C.
- c. The rate of production of turbulent kinetic energy is proportional to the vertical gradient of the horizontal velocity at the free surface, $\partial u/\partial z|_{z=\eta}$.
- d. Breaking-induced turbulence is primarily convected in the near-surface region with the horizontal velocity at the free surface.

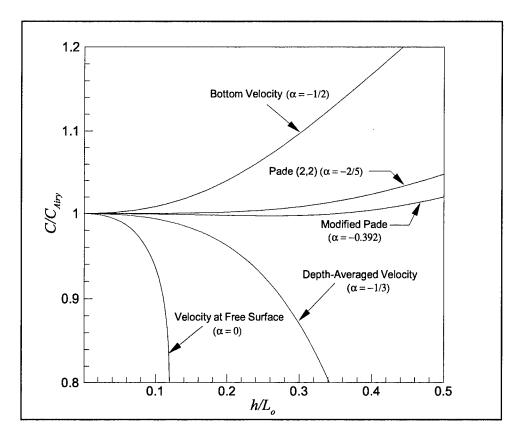


Figure 1 Comparison of normalized phase speeds for different values of α

wave train consisting of two small amplitude periodic waves with amplitudes, a_1 and a_2 , frequencies, ω_1 and ω_2 , wave numbers, k_1 and k_2 , and propagating in directions θ_1 and θ_2 respectively. The water-surface elevation can be written as:

$$\eta^{(1)}(\boldsymbol{x},t) = a_1 \cos(\boldsymbol{k}_1 \cdot \boldsymbol{x} - \omega_1 t) + a_2 \cos(\boldsymbol{k}_2 \cdot \boldsymbol{x} - \omega_2 t)$$
 (11)

where $k = (k\cos\theta, k\sin\theta)$. The second-order wave will consist of a subharmonic at the difference frequency, $\omega_{-} = \omega_{1} - \omega_{2}$, and higher harmonics at the sum frequencies $2\omega_{1}$, $2\omega_{2}$ and $\omega_{+} = \omega_{1} + \omega_{2}$. This can be written as:

$$\eta^{(2)}(\mathbf{x},t) = \frac{a_1^2}{2} G_+(\omega_1, \omega_1, \theta_1, \theta_1) \left(\cos(2\mathbf{k}_1 \cdot \mathbf{x} - 2\omega_1 t) + \frac{a_2^2}{2} G_+(\omega_2, \omega_2, \theta_2, \theta_2) \cos(2\mathbf{k}_2 \cdot \mathbf{x} - 2\omega_2 t) + a_1 a_2 G_+(\omega_1, \omega_2, \theta_1, \theta_2) \cos(2\mathbf{k}_2 \cdot \mathbf{x} - 2\omega_2 t) \right)$$
(12)

where $\mathbf{k}_{\pm} = \mathbf{k}_{1} \pm \mathbf{k}_{2}$, and $G_{\pm}(\omega_{1}, \omega_{2}, \theta_{1}, \theta_{2})$ is a bidirectional quadratic transfer function that relates the amplitude of the second-order waves to the amplitude of the first-order waves. Dean and Sharma (1981) derived expressions for the bidirectional quadratic transfer function based on second-order Stokes theory. Nwogu

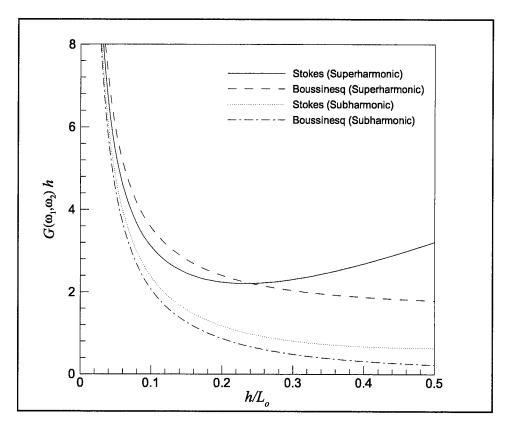


Figure 2. Comparison of quadratic transfer function for Boussinesq and Stokes theories

The effect of wave energy dissipation due to breaking is simulated in the Boussinesq model by introducing an eddy viscosity term to the right-hand side of the momentum equation (Equation 5 or 8). Nwogu (1996) used a dissipative term of the following form:

$$F_{breaking} = -v_t \nabla(\nabla u_\alpha)$$
 (15)

where v_t is the turbulent eddy viscosity. As pointed out by Kennedy et al. (2000), it is important for the dissipative term to dissipate energy but conserve momentum to accurately capture details of the mean flow field associated with breaking waves. A modified form of the dissipative term that ensures that momentum is conserved can be written as:

$$F_{breaking} = -\frac{1}{h+\eta} \nabla \{ \mathbf{v}_{t}(h+\eta) \nabla \cdot \mathbf{u}_{\alpha} \}$$
 (16)

The eddy viscosity is determined from the amount of turbulent kinetic energy, k, produced by wave breaking, and a turbulence length scale, l_t , using:

$$\mathbf{v}_t = \sqrt{k}I_t \tag{17}$$

A one-equation model is used to describe the production, advection, diffusion, and dissipation of the turbulent kinetic energy produced by wave breaking:

$$k_{t} = -\mathbf{u}_{\eta} \cdot \nabla k + \sigma \nabla \cdot \nabla (\mathbf{v}_{t} k) + B \frac{l_{t}^{2}}{\sqrt{C_{D}}} \left[\left(\frac{\partial u}{\partial z} \right)^{2} + \left(\frac{\partial v}{\partial z} \right)^{2} \right]_{z=\eta}^{3/2} - C_{D} \frac{k^{3/2}}{l_{t}}$$
(18)

The waves are assumed to start breaking when the horizontal component of the orbital velocity at the free surface, u_{η} , exceeds the phase velocity of the waves, C. The parameter B is introduced to ensure that production of turbulence occurs after the waves break, i.e.,

$$B = \begin{cases} 0 & |\boldsymbol{u}_{\eta}| < C \\ 1 & |\boldsymbol{u}_{\eta}| \ge C \end{cases}$$
 (19)

The phase velocity is determined from the linear dispersion relation (Equation 10) using the average zero-crossing period of the incident wave train. While this approach leads to some waves in an irregular wave train breaking at slightly different locations in the model than they would in nature, it was found to be more stable than trying to estimate a time-dependent phase velocity using expressions such as $C(t) = -\eta_t/|\nabla \eta|$.

The empirical constants C_D and σ have been chosen as 0.02 and 0.2 respectively. The turbulent length scale, l_t , remains the only free parameter in the turbulence model and is determined from comparisons of numerical model results with experimental data. Recommended values are the significant wave height ($l_t = H_{\text{mo}}$) for irregular waves, and the wave height ($l_t = H$) for regular waves.

Bottom Friction

The bottom boundary layer in wave fields is typically confined to a tiny region above the seabed, unlike river and tidal flows where it extends all the way up to the free surface. There is, thus, very little wave energy attenuation due to bottom friction over typical wave propagation distances of O (1km) used in Boussinesq-type models. The bottom friction factor, however, plays a more important role in wave transformation close to the shoreline and nearshore circulation patterns. The effect of energy dissipation due to a turbulent boundary layer at the seabed has been modeled by adding a bottom shear stress term to the right-hand side of the momentum equation (Equation 5 or 8):

$$F_{bfriction} = -\frac{1}{h+\eta} f_w \mathbf{u}_\alpha |\mathbf{u}_\alpha|$$
 (20)

where f_w is the wave friction factor. The bottom friction term can also be written in terms of the Chezy coefficient, C_f , used in tidal flows by replacing f_w with g/C_f^2 .

Equation 20 has been expressed in terms of u_{α} instead of the velocity at the seabed, u_b , to minimize the additional computational expense of evaluating u_b . The values of the friction factors specified in the model would thus be slightly different than those based on the bottom velocity.

3 Numerical Solution

Finite Difference Scheme

The weakly and fully nonlinear Boussinesq equations (Equations 4-9) are solved in the time-domain using a finite-difference method. The computational domain is discretized as a rectangular grid with grid sizes Δx and Δy , in the x and y directions, respectively. The equation variables η , u_{α} , and v_{α} are defined at the grid points in a staggered manner as shown in Figure 3. The water depth and surface elevation are defined at grid points (i,j), while the velocities are defined half a grid point on either side of the elevation grid points. The external boundaries of the computational domain correspond to velocity grid points.

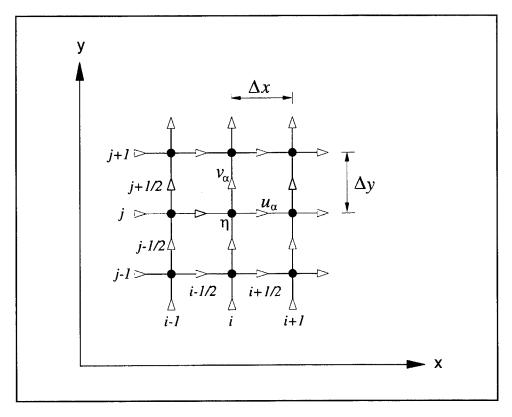


Figure 3. Computational grid for finite difference scheme

The numerical solution scheme is an implicit Crank-Nicolson scheme with a predictor-corrector method used to provide the initial estimate. The first step in the solution scheme is the predictor step in which values of the variables at an intermediate time-step $t = (n + \frac{1}{2})\Delta t$ are determined using known values at $t = n\Delta t$ (Δt is the time-step size). The second step is the corrector step in which predicted values at $t = (n + \frac{1}{2})\Delta t$ are used to provide an initial estimate of the values at $t = (n+1)\Delta t$. The last step is an iterative Crank-Nicolson scheme, which is repeated until convergence.

The partial derivatives are approximated using a forward difference scheme for time and central difference schemes for the spatial variables. The resulting Crank-Nicolson formulation for the weakly nonlinear form of the mass and momentum equations (Equations 4-6) can be written as:

$$\delta_t \eta = - \delta_x^{(1)} u_f^{n+1/2} - \delta_y^{(1)} v_f^{n+1/2}$$
(21)

$$\delta_{t}\left(u_{\alpha} + f_{4}\delta_{x}^{(2)}u_{\alpha} + f_{2}\delta_{xx}u_{\alpha}\right) = -g\delta_{x}^{(1)}\eta^{n+1/2} - \frac{1}{2}\delta_{x}^{(1)}\left[\left(\overline{u_{\alpha}^{n+1/2}}^{x}\right)^{2}\right] - \delta_{y}^{(1)}\left(\overline{v_{\alpha}^{n+1/2}}^{x} \overline{u_{\alpha}^{n+1/2}}^{y}\right) - f_{4}\left[\delta_{y}^{(1)}(h) \ \delta_{t}\delta_{x}^{(1)}\left(\overline{v_{\alpha}^{n+1/2}}^{y}\right) + \delta_{x}^{(1)}(h) \ \delta_{t}\delta_{y}^{(1)}\left(\overline{v_{\alpha}^{n+1/2}}^{x}\right)\right] - f_{2}\delta_{t}\delta_{xy}v_{\alpha}^{n+1/2}$$

$$(22)$$

$$\delta_{t}\left(v_{\alpha} + f_{4}\delta_{y}^{(2)}v_{\alpha} + f_{2}\delta_{yy}v_{\alpha}\right) = -g\delta_{y}^{(1)}\eta^{n+1/2} - \frac{1}{2}\delta_{y}^{(1)}\left[\left(\overline{v_{\alpha}^{n+1/2}}^{y}\right)^{2}\right] - \delta_{x}^{(1)}\left(\overline{v_{\alpha}^{n+1/2}}^{x} \overline{u_{\alpha}^{n+1/2}}^{y}\right)$$

$$- f_{4}\left[\delta_{y}^{(1)}(h) \ \delta_{t}\delta_{x}^{(1)}\left(\overline{u_{\alpha}^{n+1/2}}^{y}\right) + \delta_{x}^{(1)}(h) \ \delta_{t}\delta_{y}^{(1)}\left(\overline{u_{\alpha}^{n+1/2}}^{x}\right)\right] (23)$$

$$- f_{2}\delta_{t}\delta_{xy}u_{\alpha}^{n+1/2}$$

where the volume flux densities u_f and v_f are given by:

$$u_{f\,i+1/2,j} = \overline{h+\eta}^{x} u_{\alpha\,i+1/2,j} + \overline{h}^{x} f_{1} \Big(\delta_{xx} u_{\alpha} + \delta_{xy} v_{\alpha} \Big)$$

$$+ \overline{h}^{x} f_{3} \Big[2 \delta_{x}^{(1)}(h) \delta_{x}^{(2)} u_{\alpha} + \delta_{x}^{(1)}(h) \delta_{y}^{(1)} \Big(\overline{v_{\alpha}}^{x} \Big) + \delta_{y}^{(1)}(h) \delta_{x}^{(1)} \Big(\overline{v_{\alpha}}^{y} \Big) \Big]$$
(24)

$$v_{fi,j+1/2} = \overline{h+\eta}^{y} v_{\alpha i,j+1/2} + \overline{h}^{y} f_{1} \left(\delta_{xy} u_{\alpha} + \delta_{yy} v_{\alpha} \right) + \overline{h}^{y} f_{3} \left[2 \delta_{y}^{(1)}(h) \delta_{y}^{(2)} v_{\alpha} + \delta_{x}^{(1)}(h) \delta_{y}^{(1)} \left(\overline{u_{\alpha}}^{x} \right) + \delta_{y}^{(1)}(h) \delta_{x}^{(1)} \left(\overline{u_{\alpha}}^{y} \right) \right]$$
(25)

The parameters f_1 to f_4 are given by:

$$f_1 = \left[\frac{(z_\alpha + h)^2}{2} - \frac{h^2}{6} \right] \tag{26a}$$

$$f_2 = \left[\frac{(z_\alpha + h)^2}{2} - \frac{h^2}{2} \right] \tag{26b}$$

$$f_3 = \left[(z_\alpha + h) - \frac{h}{2} \right] \tag{26c}$$

$$f_4 = \left[(z_\alpha + h) - h \right] \tag{26d}$$

The average and difference operators in Equations 21 to 25 are given by:

$$\delta_t \phi = \frac{1}{\Delta t} (\phi^{n+1} - \phi^n) \tag{27a}$$

$$\phi^{n+1/2} = \frac{1}{2} (\phi^n + \phi^{n+1})$$
 (27b)

$$\overline{\phi}^{x} = \frac{1}{2} (\phi_{i+1,j} + \phi_{i,j}) \quad or \quad \frac{1}{2} (\phi_{i+1/2,j} + \phi_{i-1/2,j})$$
 (27c)

$$\overline{\phi}^{y} = \frac{1}{2} (\phi_{i,j+1} + \phi_{i,j}) \quad or \quad \frac{1}{2} (\phi_{i,j+1/2} + \phi_{i,j-1/2})$$
 (27d)

$$\delta_x^{(1)} \phi = \frac{1}{\Delta x} \left(\phi_{i+1,j} - \phi_{i,j} \right) \text{ or } \frac{1}{\Delta x} \left(\phi_{i+1/2,j} - \phi_{i-1/2,j} \right)$$
 (27e)

$$\delta_{y}^{(1)} \phi = \frac{1}{\Delta y} (\phi_{i,j+1} - \phi_{i,j}) \text{ or } \frac{1}{\Delta y} (\phi_{i,j+1/2} - \phi_{i,j-1/2,j})$$
 (27f)

$$\delta_x^{(2)} \phi = \frac{1}{2\Delta x} \left(\phi_{i+3/2,j} - \phi_{i-1/2,j} \right) \tag{27g}$$

$$\delta_{y}^{(2)} \phi = \frac{1}{2\Delta \nu} \left(\phi_{i,j+3/2} - \phi_{i,j-1/2} \right) \tag{27h}$$

$$\delta_{xx} \phi = \frac{1}{\Delta x^2} \left(\phi_{i+3/2,j} - 2\phi_{i+1/2,j} + \phi_{i-1/2,j} \right)$$
 (27i)

$$\delta_{yy}\phi = \frac{1}{\Delta v^2} \left(\phi_{i,j+3/2} - 2\phi_{i,j+1/2} + \phi_{i,j-1/2} \right)$$
 (27j)

$$\delta_{xy}\phi = \frac{1}{\Delta x \Delta v} \left(\phi_{i,j+1} - 2\phi_{i,j} + \phi_{i,j-1} \right)$$
 (27k)

and ϕ represents the variables $(\eta, u_{\alpha}, v_{\alpha})$. The finite-difference operator definitions in Equation 27 corresponding to the x and y components of the momentum equation are centered at (i+1/2,j) and (i,j+1/2), respectively.

The finite difference formulation of the continuity equation (Equation 21) yields an algebraic equation that is explicitly solved for η at all grid points. The formulation for the x and y momentum equations (Equations 22 and 23) have been decoupled by placing the v_{xt} , v_{yt} , and v_{xyt} terms on the right-hand side of the x equation and the u_{xt} , u_{yt} , and u_{xyt} terms on the right-hand side of the y equation. This reduces the momentum equations to tridiagonal equations for u_{α} and v_{α} along lines in the x and y direction, respectively. Tridiagonal matrices are much easier to store and solve than the large sparse matrix equation that would be obtained if the equations were not decoupled. The major disadvantage of this approach, however, is that the iterative step takes longer to converge for shorter-period waves propagating at large angles to the grid where the higher-order cross-derivative terms (u_{xyt}, v_{xyt}) become comparable in magnitude to the inline derivative terms (u_{xxt}, v_{yyt}) .

The numerical scheme is stable provided that the Courant number, C_R , is less than 1, i.e.,

$$C_R = \sqrt{\left[C^2 \Delta t^2 \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2}\right)\right]} < 1$$
 (28)

where C is the phase speed based on the average zero-crossing period of the incident waves. It is, however, recommended that the Courant number be kept within the range 0.5 to 0.7 since nonlinear wave-wave interactions, wave breaking, and the presence of reflected waves can affect the stability criterion of the numerical model.

Boundary Conditions

To solve the governing equations, appropriate boundary conditions have to be imposed at the boundaries of the computational domain. This requires specification of waves propagating into the domain and the absorption of waves propagating out of the domain. The equations have also been modified to simulate wave interaction with fully/partially reflecting structures within the computational domain. The types of boundaries considered in BOUSS-2D include:

- a. Fully reflecting or solid wall boundaries.
- b. External wave generation boundaries.
- c. Internal wave generation boundaries.
- d. Wave absorption or damping regions.
- e. Porous structures.

Solid wall boundaries

Along solid wall or fully reflecting boundaries, the horizontal velocity normal to the boundary must be zero over the entire water depth, i.e.,

$$\mathbf{u} \cdot \mathbf{n} = 0 \qquad -h < z < \eta \tag{29}$$

where n is the normal vector to the boundary. This condition is satisfied in the depth-integrated equations by specifying that both the volume flux density and velocity normal to the boundary are zero, i.e.,

$$\boldsymbol{u}_{\alpha} \cdot \boldsymbol{n} = 0 \tag{30}$$

$$\boldsymbol{u}_f \cdot \boldsymbol{n} = 0 \tag{31}$$

Since the equations are solved on a staggered grid, the boundary conditions are specified as either $u_{\alpha} = u_f = 0$ along wall boundaries perpendicular to the x-axis, or $v_{\alpha} = v_f = 0$ along wall boundaries perpendicular to the y-axis.

External wave generation boundaries

Along external wave generation boundaries, time-histories of velocities u_{α} or v_{α} , and flux densities u_f or v_f corresponding to an incident storm condition are specified. The time-histories may correspond to regular or irregular, unidirectional or multidirectional waves.

Regular Waves. Regular, long-crested wave conditions are specified in terms of a wave height, H, wave period, T, and direction of propagation, θ . The water-surface elevation for small-amplitude waves (H << h) may be written as:

$$\eta(x, y, t) = \frac{H}{2} \cos(kx \cos\theta + ky \sin\theta - \omega t)$$
 (32)

where $\omega = 2\pi/T$ is the angular frequency, k is the wave number, and θ is the direction of wave propagation relative to the positive x-axis. The boundary conditions along a wave generation line perpendicular to the x-axis may be obtained from the linearized form of the continuity equation (Equation 5) for water of constant depth as:

$$u_{\alpha}(x_g, y_g, t) = T_{\mu}(\omega)\cos\theta \quad \eta(x_g, y_g, t)$$
 (33)

$$u_f(x_g, y_g, t) = \left[(h + \eta) - h \left(\frac{\alpha_2^2}{2} - \frac{1}{6} \right) (kh)^2 \right] u_\alpha(x_g, y_g, t)$$
 (34)

where (x_g, y_g) are the x-y coordinates of the wave generation line and $T_u(\omega)$ is a linear transfer function given by:

$$T_{u}(\omega) = \frac{\omega}{kh\left[1-\left(\frac{\alpha_{2}^{2}}{2}-\frac{1}{6}\right)(kh)^{2}\right]}$$
(35)

and $\alpha_2 = (z_{\alpha} + h)/h$. Similar expressions apply to v_{α} and v_f for wave generation lines perpendicular to the y-axis with $\cos\theta$ replaced by $\sin\theta$ in Equation 33.

For large amplitude waves [H=O(h)], higher harmonic components $(2\omega, 3\omega,$ etc.) are generated due to the nonlinear terms in the governing equations. These waves are often called bound waves since they are attached to the primary wave and travel at its phase speed, $C=\omega/k$, instead of the phase speed of a free wave at the corresponding frequency. The wave shape also changes from the sinusoidal shape assumed in Equation 32 to an asymmetric one with peaked crests and broad shallow troughs. If linear wave conditions are imposed at the boundaries, the numerical model will generate free higher harmonic components with the same magnitude but 180 deg out of phase with the bound waves at the wavemaker to satisfy the linear boundary condition. The presence of bound and free higher frequency waves that travel at different speeds will lead to a spatially nonhomogenous wave field with the wave height and shape changing continuously over the computational domain.

The Fourier approximation method of Rienecker and Fenton (1981) has been used to solve the weakly nonlinear form of the Boussinesq equations and develop nonlinear boundary conditions for the generation of large-amplitude regular waves in shallow water. The partial differential Equations 4 to 6 are initially transformed into a set of coupled nonlinear ordinary differential equations in terms of a moving coordinate system, $\xi = x - Ct$. The velocity variable u_{α} is expanded as a Fourier series and substituted into the governing equations, which are evaluated at a finite number of collocation points over half a wavelength to yield a system of nonlinear algebraic equations. A Newton-Raphson iterative procedure is used to solve the nonlinear equations for the unknown values of the free surface displacement at the collocation points, the Fourier coefficients, the wave number, and the phase speed. Details of the technique are provided in Appendix A.

Irregular Unidirectional Waves. For nonperiodic waves, the incident wave conditions are typically expressed in the form of a wave spectrum, which describes the frequency distribution of wave energy. Different parametric shapes have been proposed for wave spectra including:

- a. The Pierson-Moskowitz (PM) spectrum for fully developed sea states in deep water, which is defined in terms of the wind speed.
- b. The Bretschneider (1959) spectrum, which has the same shape as the PM spectrum but is defined in terms of the significant wave height and peak period.

- c. The JONSWAP spectrum for fetch-limited conditions in deep water.
- d. The TMA spectrum for fetch-limited conditions in shallow water.
- e. The Ochi-Hubble spectrum for bimodal sea states with double-peaked spectra.

Expressions for the different wave spectra are provided in Appendix B.

The Fourier series technique is used to generate time-histories of the velocity boundary conditions from the wave spectrum. The water-surface elevation, $\eta(t)$, is assumed to be a zero-mean, stationary, random Gaussian process. The surface-elevation time series at a reference point $x_r = (x_r, y_r)$ in the computational domain can be represented as a linear superposition of N regular wave components, i.e.,

$$\eta(\mathbf{x}_r, t) = \sum_{j=1}^{N} a_j \cos\left[\mathbf{k}_j \cdot \mathbf{x}_r - \omega_j t + \varepsilon_j\right]$$
(36)

where a_j , ω_j , ε_j , and $k_j = (k_j \cos \theta, k_j \sin \theta)$ are the amplitude, angular frequency, phase angle, and wave number vector of the j^{th} frequency component, respectively. The angle, θ , is the direction of wave propagation relative to the positive x-axis.

The wave spectrum is divided into N frequency bands with uniform spacing, $\Delta \omega$, so that the frequency of the j^{th} wave component is given by $\omega_j = j\Delta \omega$. The amplitudes of the individual wave components are obtained deterministically from the wave spectrum, $S_n(\omega)$, as:

$$a_j = \sqrt{2S_{\eta}(\omega_j)\Delta\omega} \tag{37}$$

while the phase angles, ε_j , are randomly selected from a uniform distribution between 0 and 2π . Incident wave conditions are more typically specified in terms of the repeat period or duration of the record, T_D , and time-step, Δt . The values of N and $\Delta \omega$ can be obtained from these as:

$$\Delta \omega = \frac{1}{T_D} \tag{38}$$

$$N = \frac{T_D}{2\Delta t} \tag{39}$$

The velocity and flux boundary conditions along a wave generation line perpendicular to the x-axis may be obtained from the surface elevation using the linear transfer function approach:

$$u_{\alpha}(\mathbf{x}_{g},t) = \sum_{j=1}^{N} T_{u}(\omega_{j}) a_{j} \cos \theta \cos \left[\mathbf{k}_{j} \cdot (\mathbf{x}_{g} - \mathbf{x}_{r}) - \omega_{j} t + \varepsilon_{j} \right]$$
(40)

$$u_f(x_g,t) = [h + \eta(x_g,t)]u_\alpha(x_g,t) + h^3 \left[\frac{\alpha_2^2}{2} - \frac{1}{6}\right] \left(u_{\alpha\alpha}(x_g,t) + v_{\alpha\alpha}(x_g,t)\right)$$
(41)

where

$$\eta(\mathbf{x}_{g},t) = \sum_{j=1}^{N} a_{j} \cos\left[\mathbf{k}_{j} \cdot (\mathbf{x}_{g} - \mathbf{x}_{r}) - \omega_{j}t + \varepsilon_{j}\right]$$
(42)

$$u_{\text{occ}}(\boldsymbol{x}_{g},t) = -\sum_{j=1}^{N} a_{j} k_{j}^{2} \cos^{3} \theta \cos \left[\boldsymbol{k}_{j} \cdot (\boldsymbol{x}_{g} - \boldsymbol{x}_{r}) - \omega_{j} t + \varepsilon_{j} \right]$$
(43)

$$V_{\alpha xy}(\mathbf{x}_g, t) = -\sum_{j=1}^{N} a_j k_j^2 \sin^2 \theta \cos \theta \cos \left[\mathbf{k}_j \cdot (\mathbf{x}_g - \mathbf{x}_r) - \omega_j t + \varepsilon_j \right]$$
 (44)

For highly nonlinear irregular waves in shallow water¹, the velocity boundary conditions would have to be modified to take into account the presence of lower and higher frequency wave components induced by nonlinear interactions between the primary wave components. Second-order Boussinesq theory can be used to generate the velocities and flux densities associated with the bound second-order waves along the wave generation boundary. However, this theory is valid over a limited range of wave steepnesses (H/L) and relative depths (h/L) because it only includes second-harmonic terms. Second-order Stokes theory, for example, cannot accurately describe the shape of cnoidal-type waves in shallow water when the Ursell parameter (HL^2/h^3) is large.

A different approach to generating steep irregular waves in shallow water is the nonlinear Fourier method of Osborne (1997), in which an irregular wave train is represented as a superposition of nonlinear cnoidal or solitary type waves. This approach, however, has not yet been implemented in BOUSS-2D.

Irregular Multidirectional Waves. Naturally occurring ocean waves exhibit a pattern that varies randomly not only in time but also in space. The wave energy is distributed over both frequency and direction and can be described in terms of a directional wave spectrum, $S_{\eta}(\omega,\theta)$, which is the product of the frequency spectrum, $S_{\eta}(\omega)$, and a directional spreading function $D(\omega,\theta)$:

$$S_{n}(\omega, \theta) = S_{n}(\omega)D(\omega, \theta)$$
 (45)

The directional spreading function is non-negative and should satisfy the following relation:

$$\int_{-\pi}^{\pi} D(\omega, \theta) = 1 \tag{46}$$

¹ A useful guideline is $H_{\rm mo}/L_p > 0.025$ tanh $k_p h$, where $H_{\rm mo}$ is the significant wave height, and L_p and k_p are respectively the wavelength and wave number based on the peak frequency of the spectrum.

One of the most commonly used models for the directional spreading function is the cosine-power function defined as:

$$D(\theta) = \frac{\Gamma(s+1)}{\sqrt{\pi} \Gamma(s+1/2)} \cos^{2s}(\theta - \theta_p) \quad \text{for } |\theta - \theta_p| < \pi/2$$
 (47)

where θ_p is the principal direction of wave propagation and Γ is the gamma function. The parameter s is an index describing the degree of directional spreading with $s \to \infty$ representing a unidirectional wave field. Figure 4 shows a plot of the of the cosine power spreading function for different values of the spreading index, s.

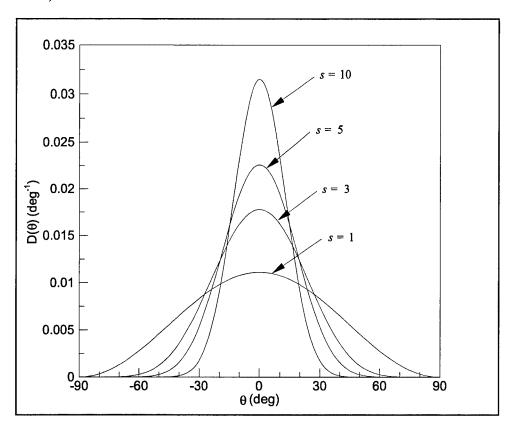


Figure 4. Cosine-power spreading function for different values of the spreading index s

A number of other models have been proposed for the directional spreading function including the normal, circular normal, and wrapped-normal distribution (Borgman 1969). A more intuitive and universal parameter to describe the degree of directional spreading in a multidirectional sea state is the standard deviation of the directional spreading function, σ_{θ} , which is defined as:

$$\sigma_{\theta}^{2} = \int_{\theta_{p}-\pi/2}^{\theta_{p}+\pi/2} D(\theta) (\theta - \theta_{p})^{2} d\theta$$
 (48)

Given the same standard deviation, there is very little difference between the shapes of different proposed forms of the directional spreading functions as shown in Appendix C.

Time-histories of the velocity boundary conditions can be synthesized from the directional wave spectrum using an extension of the linear superposition technique used for irregular, unidirectional waves. The directional wave spectrum is initially divided into N frequency bands with uniform spacing, $\Delta \omega$, and M direction bands with uniform spacing $\Delta \theta$. The water-surface elevation $\eta(x_n t)$ can be represented as a linear superposition of periodic wave components with different amplitudes and frequencies, propagating in different directions, i.e.,

$$\eta(\mathbf{x},t) = \sum_{i=1}^{N} \sum_{j=1}^{M} a_{ij} \cos\left[\mathbf{k}_{ij} \cdot \mathbf{x} - \omega_{i}t + \varepsilon_{ij}\right]$$
(49)

where $\mathbf{k}_{ij} = (k_i \cos \theta_j, k_i \sin \theta_j)$. The wave amplitudes, a_{ij} , are obtained deterministically from the directional wave spectrum as:

$$a_{ij} = \sqrt{2S_{\eta}(\omega_i, \theta_j)\Delta\omega\Delta\theta}$$
 (50)

while the phase angles, ε_{ij} , are randomly selected from a uniform distribution between 0 and 2π . For a given time series duration, T_D , and time-step, Δt , the values of N and $\Delta \omega$ can be obtained in the same manner as for unidirectional waves using Equations 38 and 39 respectively.

For finite duration time records, the double summation model (Equation 49) produces a wave field that is spatially nonhomogenous. As pointed out by Jeffreys (1987), this is because the phase difference between wave components with identical frequencies but propagating in different directions is no longer random but locked. An extreme example of this phenomenon is the standing wave pattern that is produced when incident waves are fully reflected by a vertical wall. The wave field consists of two waves with the same amplitude and frequency propagating in opposite directions with a constant phase difference between them. The wave heights vary from zero at the nodes to twice the incident wave height at the antinodes. This variability is obviously reduced by including more frequency and direction components. However, as pointed by Stansberg (1987) and others, the number of wave components required to reduce the spatial variability in wave energy to within acceptable levels is quite large [O(10,000)].

A different approach to producing a spatially homogenous multidirectional wave field is to assume that each wave component has a unique direction of propagation. Similar to an irregular unidirectional wave train, the water-surface elevation is given by Equation 36 with $k_j = (k_j \cos \theta_j, k_j \sin \theta_j)$. Miles (1989) discusses four different methods of assigning directions to each frequency component. In BOUSS-2D, the random direction method was adapted in which wave directions are selected at random from the cumulative distribution of the directional spreading function. With this technique, the frequency spectrum is matched exactly. However, the directional spreading function is matched only in

a global sense over the entire record. The method also does not guarantee a symmetric directional distribution even when the target distribution is symmetric.

The velocity and flux boundary conditions along the wave generation lines are obtained from the surface elevation time-histories using the linear transfer function approach described previously in Equations 40 to 44.

Internal wave generation boundaries

In applications where there is significant wave reflection from bathymetric features or structures within the computational domain, it is desirable to absorb the waves that propagate back to the wave generation boundary to prevent a buildup of wave energy inside the domain. This can be achieved by modifying the boundary conditions along the wave generation boundary to simultaneously generate and absorb reflected waves (e.g., Van Dongeren and Svendsen 1997). A different approach proposed by Larsen and Dancy (1983) is to generate the waves inside the computational domain and absorb reflected waves in a damping layer placed behind the generation boundary. This approach has been adopted in BOUSS-2D with the governing equations modified to allow for the generation of waves inside the computational domain.

Consider the generation of waves along a horizontal line by a distribution of sources that extend from the seabed (z = -h) to the free surface $(z = \eta)$. The velocity potential associated with the fluid motion satisfies the Laplace equation everywhere in the fluid except for generation line $(x = x_g)$ where there is a point source of fluid mass. The governing equation for the fluid motion can thus be written as:

$$\nabla^2 \phi = q(y, z, t) \delta(x - x_g)$$
 (51)

where q(y,z,t) is the volume flux density. Assuming that the water depth is constant along the generation line, a modified form of the second-order Taylor series expansion of the velocity potential about an arbitrary elevation $z = z_{\alpha}$ in the water column (Equation 1) can be written as:

$$\phi = \phi_{\alpha} + \frac{1}{2} \left[\left(z_{\alpha} + h \right)^{2} - \left(z + h \right)^{2} \right] \left[\nabla^{2} \phi_{\alpha} - q \delta(x - x_{g}) \right]$$
 (52)

The horizontal fluid velocities are obtained from the velocity potential as:

$$\boldsymbol{u} = \nabla \phi_{\alpha} + \frac{1}{2} \left[\left(z_{\alpha} + h \right)^{2} - \left(z + h \right)^{2} \right] \nabla \left[\nabla^{2} \phi_{\alpha} - q \delta(x - x_{g}) \right]$$
 (53)

On a rectangular grid with a finite grid spacing Δx , the delta function can be replaced with $2/\Delta x$. To generate waves with a given velocity profile $u_o(y,z,t)$, the mass and momentum equations along the grid generation line and adjacent velocity points can be written as:

$$\eta_t + \nabla \cdot \int_{-h}^{\eta} u \ dz = \frac{2}{\Delta x} \int_{-h}^{\eta} u_o \ dz \tag{54}$$

$$\boldsymbol{u}_{\alpha t} + g \nabla \eta + (\boldsymbol{u}_{\alpha} \cdot \nabla) \boldsymbol{u}_{\alpha} + \frac{1}{2} \left[(z_{\alpha} + h)^{2} - h^{2} \right] \left[\nabla (\nabla \cdot \boldsymbol{u}_{\alpha t} - 2u_{\alpha t} / \Delta x) \right] = 0 \quad (55)$$

Some previous investigators (e.g., Larsen and Dancy 1983) introduced a point source for fluid flow into the continuity equation. It is, however, important to apply a correction to the momentum equations to account for higher-order spatial derivatives across the generation line.

Damping regions

Waves propagating out of the computational domain are absorbed in damping regions placed around the perimeter of the computational domain. Damping layers can also be used to model the partial reflection from harbor structures inside the computational area. Artificial dissipation of wave energy in damping layers is achieved through the introduction of a term proportional to the surface elevation into the right-hand side of the mass equation:

$$F_{damping_{-}\eta} = -\mu(x)\eta \tag{56}$$

and a term proportional horizontal velocity into the right-hand side of the momentum equation:

$$F_{damping \ u} = -\mu(x) u_{\alpha} \tag{57}$$

where $\mu(x)$ is the damping strength with units of s⁻¹. Introduction of the damping terms lead to the nonconservation of mass and momentum in the damping regions. However, extensive tests with different combinations of the damping terms showed that the inclusion of damping terms in both the mass and momentum equation was more effective than just a damping term in the momentum equation.

Numerical simulations to evaluate the performance of the damping layer showed that waves could be effectively damped out in a layer half a wavelength wide by employing a quadratic variation of $\mu(x)$ with a peak value of 30/T, where T is the wave period. The damping strength has thus been nondimensionalized by 30/T, i.e.,

$$\mu_{nd}(\mathbf{x}) = \frac{T}{30}\mu(\mathbf{x}) \tag{58}$$

where $\mu_{nd}(x)$ is a nondimensional damping coefficient that is allowed to vary from 0 to 1. Figure 5 shows the variation of the reflection coefficient with damping coefficient for different relative widths (w/L) of the damping layer, where w is the width of the damping layer and L is the wavelength. It should be pointed

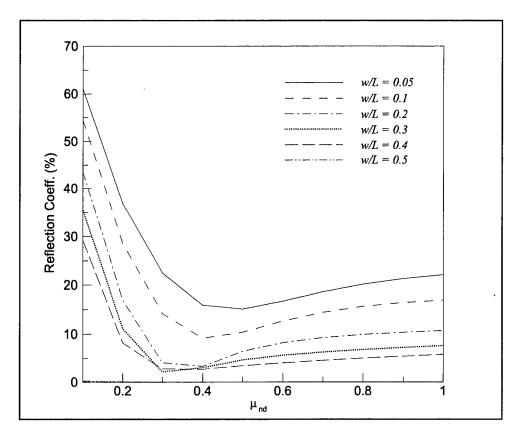


Figure 5. Variation of reflection coefficient with damping coefficient

out that the results presented in Figure 5 are for normally incident waves. Different reflection coefficients would be obtained for obliquely incident waves.

Flow through porous structures

The Boussinesq equations have also been modified to simulate partial wave reflection and transmission through surface-piercing porous structures such as breakwaters. The modified equations for the porous region can be written in terms of either the velocity in the pores or the volume-averaged (discharge) velocity. In order to easily match velocities and fluxes across the water/porous structure interface, the equations for the porous region are written in terms of the discharge velocity. Ignoring inertial effects, the modified form of the equations for the porous region are obtained by replacing \boldsymbol{u} with \boldsymbol{u}/n , where n is the porosity, and including a term to account for energy dissipation inside the structure:

$$\eta_t + \nabla \cdot \left(\frac{u_f}{n}\right) = 0 \tag{59}$$

$$u_{\alpha,t} + ng\nabla\eta + u_{\alpha}\cdot\nabla\left(\frac{u_{\alpha}}{n}\right) + z_{\alpha}\left[\nabla\left(u_{\alpha,t}\cdot\nabla h\right) + (\nabla\cdot u_{\alpha,t})\nabla h\right] + \frac{1}{2}\left[\left(z_{\alpha} + h\right)^{2} - h^{2}\right]\nabla\left(\nabla\cdot u_{\alpha,t}\right) + nf_{l}u_{\alpha} + nf_{t}u_{\alpha}|u_{\alpha}| = 0$$
(60)

where f_1 and f_2 are laminar and turbulent friction factors respectively. Engelund (1953) recommended the following empirical relationships for the laminar and turbulent friction factors:

$$f_{l} = \alpha_{o} \frac{(1-n)^{3}}{n^{2}} \frac{v}{d^{2}}$$
 (61)

$$f_{t} = \beta_{o} \frac{(1-n)}{n^{3}} \frac{1}{d} \tag{62}$$

where v is the kinematic viscosity of water, d is the characteristic stone size, and α_o and β_o are empirical constants that range from 780 to 1,500, and 1.8 to 3.6 respectively.

Simulation of Wave Runup

The runup of waves on shorelines provides an important boundary condition for predicting wave-induced currents and sediment transport in the surf zone. The runup limit is also important for determining the minimum crest elevation of coastal structures to prevent overtopping and/or flooding. A simple runup scheme has been implemented in BOUSS-2D. Dry computational cells (land points) are assumed to be porous regions where the phreatic surface elevation and volume-averaged velocities are calculated simultaneously with the fluid motion in the wet cells. When the phreatic surface elevation exceeds the elevation of the land point by a specified threshold, the porous cell is considered flooded and treated as a wet cell during the next time-step. Alternatively, when the free surface elevation drops below a specified threshold above the bottom elevation of a wet cell, the wet cell is assumed to be dry and treated as a porous cell during the next time-step.

Subgrid Turbulence

BOUSS-2D optionally provides a mechanism to simulate the turbulence and mixing that occurs in regions with large gradients in the horizontal velocities such as around the tips of breakwaters. The dissipation term is identical to that used for wave breaking, i.e., Equation 16. The eddy viscosity is given by Smagorinsky's (1963) formulation with the turbulent length scale proportional to the grid size. It can be written as:

$$v_{t} = C_{s}^{2} \Delta x \Delta y \left[\left(u_{\alpha,x} \right)^{2} + \left(v_{\alpha,y} \right)^{2} + \frac{1}{2} \left(u_{\alpha,y} + v_{\alpha,x} \right)^{2} \right]$$
 (63)

where C_s is an empirical constant.

4 Setting Up and Running BOUSS-2D

BOUSS-2D is a high-resolution wave model designed for investigating complex wave transformation problems over small regions (1-5 km). It is ideally suited for applications where reflection, diffraction, and/or nonlinear interactions are significant such as near coastal inlets and harbors. For wave propagation over large open areas where the processes of wind-wave generation, shoaling and refraction are dominant, phase-averaged models such as STWAVE (Smith, Sherlock, and Resio 2001) should be used. For periodic harbor oscillations, frequency-domain models such as the elliptic mild-slope model CGWAVE (Demirbilek and Panchang 1998) should be used since time-domain models take longer than frequency-domain models to attain steady-state conditions.

Overview of Model Setup

The basic steps involved in setting up and running BOUSS-2D are:

- a. Collect ancillary data such as bathymetric data and wave climate information.
- b. Select portion of the ocean to be covered by the numerical model and prepare 2-D rectangular grids containing information on the:
 - (1) Seabed elevations over the computational area.
 - (2) Damping values for the absorption of outgoing waves at model boundaries (optional).
 - (3) Porosity values if porous structures such as breakwaters are inside the computational domain (optional).
 - (4) Tidal current distribution over the computational area (optional).
- c. Create a simulation parameter file that contains all the information required to run the model. This can be done using the DOS-based interactive program Pre-BOUSS2D or other Windows-based programs.
- d. Run the BOUSS-2D model.
- e. Analyze the model output and plot the results.

Collection of Bathymetric and Wave Climate Data

The first step in the modeling process is the collection of information on the seabed elevations over the computational area. This can be obtained from hydrographic surveys of the area, digitizing nautical charts, or from digital topographic databases such as those maintained by the National Oceanic and Atmospheric Administration (NOAA).

Wave climate information close to the project site can be obtained from:

- a. Long-term wave measurements at the project location.
- b. Long-term wave measurements in deeper water with buoys such as those operated by NOAA.
- c. Hindcast from long-term wind observations using models such as Wave Model (WAM), Wave Information Steady Wave Model (WISWAVE), or Steady-State Wave Model (STWAVE).

Depending on the source of the wave climate data, simpler wave propagation models such as STWAVE (Smith, Sherlock, and Resio 2001) or Refraction/Diffraction Model for Spectral Wave Conditioning (REFDIF-S) (Kirby and Ozkan 1994) might have to be run to transfer the wave climate data to the boundary of the computational grid. Statistical techniques (e.g., Borgman 1972) can then be used to reduce the wave climate data to design wave conditions with associated return periods.

Information on tidal water levels and currents near the project site can be obtained using prediction techniques based on long-term tidal observations (e.g., NOAA) or by running more sophisticated circulation models such as Advanced Circulation (ADCIRC) Model for Oceanic, Coastal and Estuarine Waters. If the current speeds exceed 10 percent of the phase velocity of the waves, the currents could significantly modify the wave field and a 2-D circulation model would have to be run to provide the spatial distribution of current speeds over the computational area.

Preparation of Bathymetric Grid File

BOUSS-2D simulates wave propagation over a 2-D Cartesian grid as shown in Figure 6. The computational domain is defined as a rectangular region from $(x_{\text{origin}}, y_{\text{origin}})$ to $(x_{\text{max}}, y_{\text{max}})$ with uniform grid spacings Δx and Δy in the x and y directions, respectively. The bathymetric grid represents the seabed elevation at each node of the grid with land points defined as positive while water points are defined as negative. To prepare the grid, the spatial extent and spacing of the computational grid have to be selected. Factors to consider in the selection of the grid boundaries and spacing include:

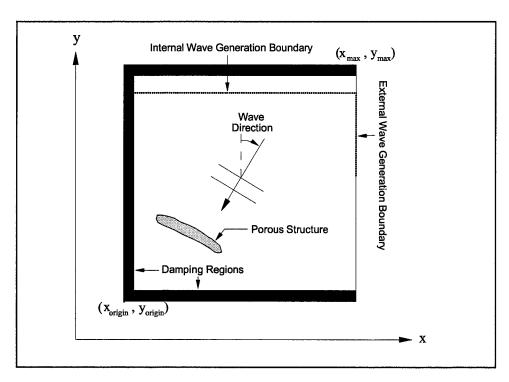


Figure 6. Definition sketch for computational grid

- a. The grid axes should be aligned as much as possible with the predominant wave direction.
- b. Points of interest in the computational domain should be kept at least one wavelength away from the boundaries to minimize the effect of diffraction into the damping layers.
- c. The water depth should be uniform along the wave generation boundary.
- d. The grid spacing should be chosen to resolve the shortest wave period of interest (T_{\min}) in the shallowest part of the domain (h_{\min}) . This typically corresponds to having at least eight grid points per wavelength in the shallow regions and 20 to 30 points per wavelength at the peak wave period (T_p) in the deep regions (h_{\max}) .
- e. The maximum water depth has to be less than half the shortest wavelength of interest $(h_{\text{max}} \le L(T_{\text{min}})/2)$. In regions with relatively deep water along the offshore boundary, an artificial maximum depth can be imposed in the numerical model to ensure that the shortest waves of interest are resolved. For example, if we are interested in modeling a sea state with $T_p = 10 \text{ s}$ and $T_{\text{min}} = 6 \text{ s}$ over an area where the water depth ranges from 5 m to 100 m, a maximum depth of 28 m can be imposed corresponding to $L(T_{\text{min}})/2$.
- f. The maximum size of the computational area should be based on the amount of available computational resources. For typical PC's or workstations with 100 to 200 MB of virtual memory, the grid size should not exceed 500 x 500 grid points. Larger grids can be used at the cost of much longer computational times.

Once the grid spacing and extent have been chosen, different algorithms (linear, inverse distance, kriging, etc.) can be used to interpolate the seabed elevation data (x,y,z) onto a uniform rectangular grid. Land regions and impermeable harbor structures are then mapped onto the grid as positive elevations. The grid data should then be saved as an ASCII file in the grid file format described in Appendix D.

Preparation of Damping Grid File

The external boundaries of the computational grid are considered to be fully reflecting wall boundaries unless it is specified as a wave generation boundary. Damping regions have to be placed inside the domain to absorb outgoing waves. The damping regions should be of the order of half a wavelength wide with a quadratic variation of the nondimensional damping coefficient, $\mu_{nd}(x,y)$, from 0 to 1 at the wall boundary.

A utility program GEN_DAMP (Appendix E) has been provided to generate the damping file given the location of the damping layers (North, South, East, or West grid boundaries), the width of the damping layer, and the nondimensional damping strength at the end wall. The damping file is stored as an ASCII file in the grid file format described in Appendix D.

Preparation of Porosity Grid File

Porosity layers are used to simulate partial reflection and transmission through porous structures such as breakwaters. The porosity grid file contains information on the porosity distribution n(x,y) over the computational grid with a value of 1.0 for water points. A porosity value of 0.4 is typically used for breakwaters. Regions with small porosity values (n < 0.1) such as breakwater core layers should be treated as impermeable regions and mapped as land points in the bathymetry file.

A utility program MAP_POROSITY (Appendix E) has been provided to create a porosity file given the breakwater boundaries as a set of discrete (x,y) points. The porosity file should be saved as an ASCII file in the grid file format described in Appendix D.

Creation of Simulation Parameter File

All the input parameters required to run BOUSS-2D is stored in an ASCII text file, referred to as a simulation parameter file (.par). The file is a free format file with names of the simulation parameters and associated values not constrained to any particular rows or columns. The full colon (:) character is used at the beginning of lines containing parameter names and values, and the pound (#) character is used to delineate sections of a line with comments. Due to the multitude of options available for the input file, it is recommended that the interactive program Pre_BOUSS2D be used to create it. Pre_BOUSS2D can be run

from an MS-DOS prompt window by typing the program name including the filepath, e.g.,

C:\BOUSS2D\BIN\pre bouss2d

The user then interactively types in answers on the keyboard in response to questions posed by the program. Default answers shown in square brackets [...] can be selected by hitting the enter key.

Step 1. Simulation Parameter File

• Enter the name of the output simulation parameter file (.par)

Step 2. Bathymetric Information

- Enter the name of the bathymetry file (.grd)
- Enter storm surge/tidal water level offset in meters

Step 3. Damping Information

• Enter name of damping file (.grd) if there are damping regions in the computational domain

Step 4. Porous Structure Information

Enter the following information if there is a porous structure in the computational domain

- Name of porosity file (.grd)
- Characteristic stone size in porous layer (m)

Step 5. Wave Generation Boundaries

Waves may be generated along one or two boundaries. The boundaries may be external (along boundary of computational grid) or internal (within the computational grid). Internal wave generation boundaries have to be parallel to one of the grid boundaries.

For each wave generation boundary, enter the following information:

- Type of Wave Generation Boundary (External/Internal)
- For External Wave Generation Boundary
- Select grid boundary (North, East, South, or West)
- If generation line exists over part of the boundary, enter the coordinates of the start and end points.

For Internal Wave Generation Boundary

- Enter orientation of wave generation line (East-West or North-South)
- Enter the x or y coordinate of wave generation line
- If generation line exists over part of boundary, enter the coordinates of the start and end points.

Step 6. Incident Wave Information

Along wave generation boundaries, BOUSS-2D requires the horizontal velocities $u_{\alpha}(t)$ and flux densities $u_{\beta}(t)$ normal to the boundary at each time-step. The time-histories may correspond to regular or irregular, unidirectional or multidirectional waves. The velocity and flux time series can either be synthesized from parametric information (wave height, period, etc.) or derived from an input

surface-elevation time series. The information required to generate the incident wave boundary conditions is described as follows:

- Wave Synthesis Options
 - Synthesize velocity and flux time-histories from parametric information
 - Read in measured surface-elevation time series. The input file has to be in the time series file format described in Appendix D.
- Incident Wave Type
 - Regular Waves
 - Irregular Unidirectional Waves
 - Irregular Multidirectional Waves

Regular Waves

- Wave Height (m) vertical distance between the wave crest and trough. The incident wave height should not exceed 75 percent of the breaking limit given by the Miche criterion as $H_{\text{break}}/L = 0.14 \tanh kh$. When the wave height exceeds 25 percent of the breaking limit, nonlinear effects become important and the time-histories are synthesized using the Boussinesq-Fourier theory discussed in Appendix A.
- Wave Period (s) time interval between successive wave crests. The incident wave period has to be greater than the limit imposed by the dispersive properties of the Boussinesq equations, i.e., the wavelength calculated from the linear dispersion relation (Equation 10) using the wave period and maximum water depth has to be greater than twice the water depth $(L > 2h_{max})$.
- Wave Direction (deg) This is the direction the waves propagate into the computational domain from, and is defined in a clockwise manner from the northern boundary of the grid as shown in Figure 6. For example, waves propagating into the domain normal to the western boundary would have a direction of 270 deg. The incident wave direction also has to be within ± 85 deg of the normal to the wave generation boundary.
- Number of Wave Cycles This determines the time period over which output parameters such as the significant wave height and mean velocities are calculated after steady-state conditions have been established in the computational domain. The recommended range is from 10 to 50.

Irregular Waves

- Type of Wave Spectrum
 - JONSWAP
 - Bretschneider
 - Pierson-Moskowitz
 - TMA
 - Ochi-Hubble

Different spectral parameters will be input depending on the selected wave spectrum. The most commonly used parameters are described in the following paragraphs. Detailed information on the different wave spectra and their associated parameters are provided in Appendix B.

- Significant Wave Height, $H_{\rm mo}$ (m) Defined as four times the square root of the zeroth moment of the spectrum, i.e., $H_{\rm mo}=4\sqrt{m_0}$, where $m_0=\int_0^\infty S_{\rm \eta}(f)df$. $H_{\rm mo}$ is equivalent to the average height of the highest one-third of the waves ($H_{1/3}$) for moderate sea states in deep water with a Rayleigh wave height distribution. The input significant wave height should not exceed 50 percent of the breaking limit given by the Miche criterion based on the peak frequency of the spectrum, i.e., $H_{\rm mo,max}/L_p=0.07$ tanh k_ph .
- Peak Wave Period, T_p (s) Inverse of the cyclic frequency at which the wave spectrum is a maximum $(T_p = 1/f_p)$
- Minimum Wave Period, T_{\min} (s) The incident wave spectrum is set to zero at all frequencies greater than $1/T_{\min}$ with the truncated wave spectrum optionally rescaled to match the target significant wave height. The minimum wave period has to be greater than the limit imposed by the dispersive properties of the Boussinesq equations, i.e., the wavelength based on T_{\min} and h_{\max} has to be greater than twice the maximum water depth $[L(T_{\min}) > 2h_{\max}]$.
- Maximum Wave Period, $T_{\text{max}}(s)$ The incident wave spectrum is set to zero at all frequencies less than $1/T_{\text{max}}$. The maximum wave period is used to separate infragravity waves from wind-generated waves and has a default value of 25 s (prototype).
- Wave Direction (deg) This is the direction the waves propagate into the computational domain from, and is defined in a clockwise manner from the northern boundary of the grid as shown in Figure 6. For example, waves propagating into the domain normal to the western boundary would have a direction of 270 deg. The incident wave direction also has to be within ± 85 deg of the normal to the wave generation boundary.
- Synthesized Time Series Duration This is the recycling period of the Fourier series used to synthesize the time-histories and corresponds to the time period over which output parameters such as the significant wave height and mean velocities are calculated after steady-state conditions have been established in the computational domain. The recommended range is from 50 to 100 wave periods.
- Random Number Seed The seed of the random number generator used to select phase angles for the different Fourier components. Different seeds can be used to obtain different time records from the same wave spectrum.

Multidirectional Waves

In addition to specifying spectral parameters, the user has to select additional parameters to describe the directional distribution of wave energy. The different directional distributions are discussed in Appendix C.

- Type of Directional Spreading Function
 - Wrapped-Normal
 - Cosine-Power
- Standard Deviation, σ_{θ} (deg) The standard deviation of the Wrapped-Normal directional spreading function. The allowable range is from 5 deg to 50 deg with 10 deg representing narrow-band swell-type conditions and 30 deg representing broader, local wind-generated seas.
- Spreading Index, s Describes the degree of directional spreading for the Cosine-power directional distribution. The allowable range of the spreading index is from 0 to 65 with s = 2 representing broad, local wind-generated seas and s = 15 representing narrow-band swell-type conditions.
- Principal Wave Direction, θ_p (deg) This is the direction corresponding to peak of the directional spreading function. The wave direction is defined in a clockwise manner from the northern boundary of the grid as shown in Figure 6. The principal direction has to be within \pm 30 deg of the normal to the wave generation boundary.
- Maximum Propagation Direction, θ_{max} (deg) This is the maximum wave propagation direction relative to the normal to the wave generation boundary as shown in Figure 7. The directional distribution is truncated at ±θ_{max} and renormalized. As pointed out by Sand and Mynett (1987), θ_{max} also defines the limited area in the computational domain over which homogenous conditions exist, i.e., all wave directions are included. Diffraction effects will further reduce the size of the spatially homogenous region. The recommended value is two to three times the standard deviation of the directional distribution.

It should also be noted that when using more than one wave generation boundary, different spectral/directional parameters might be specified for the individual boundaries. However, the duration of the synthesized or input time record must be the same for both boundaries.

Step 7. Current Field

If tidal currents are significant over the computational area, the spatial distribution of the currents U(x,y) should be stored as an ASCII file in the grid file format (.grd) described in Appendix D. The user should then enter the name of the file containing the velocity data.

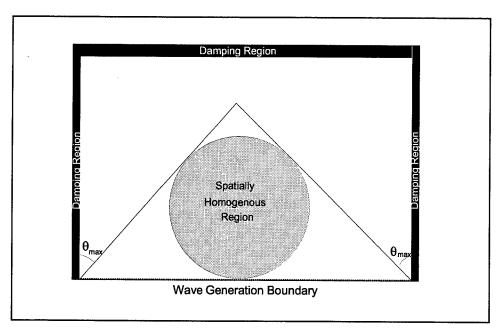


Figure 7. Sketch showing spatially homogenous region for multidirectional waves

Step 8. Simulation Parameters

- Duration of Numerical Simulation (s) This is equal to time required for the storm waves to propagate from the wave generation boundary to the farthest points of interest in the model area and establish steady-state conditions, i.e., warm-up period plus the duration of the synthesized or input time record specified in Step 6.
- Simulation Time-Step (s) The time-step should be selected based on the stability considerations, i.e., the Courant number C_r has to be less than 1.0:

$$C_r = \sqrt{\left[C^2 \Delta t^2 \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2}\right)\right]} < 1.0$$

where C is the phase velocity calculated using the maximum water depth (h_{max}) and the average zero-crossing period of the incident waves. It is recommended that the Courant number be kept within the range 0.5 to 0.7, which typically corresponds to 30 to 50 points per wave period. For plunging waves on steep slopes, it may be necessary to use up to 100 points per wave period to simulate the rapid changes in wave shape irrespective of the Courant number.

- Chezy Coefficient Bottom friction factor with a default value of 30. Should be kept between 20 and 1,000.
- Model Equations Option (Weakly Nonlinear/Fully Nonlinear) Select either weakly nonlinear model of Nwogu (1993) or the fully nonlinear model of Nwogu (1996). The fully nonlinear model is computationally more intensive

than the weakly nonlinear model and should only be used to investigate highly asymmetric waves in shallow water, wave-induced currents, and wave-current interaction.

- Wave Breaking Option (Y/N) Wave breaking should be enabled if the significant wave height is going to be greater than half the water depth in the shallowest regions of the computational area $(H_{mo} > h_{min}/2)$.
- Turbulent Length Scale, $l_t(m)$ Controls the rate of wave energy dissipation for breaking waves. Should be set equal to the significant wave height $(l_t = H_{mo})$ for irregular waves or the wave height $(l_t = H)$ for regular waves.
- Smagorinsky Constant C_s Eddy viscosity coefficient for subgrid turbulence. To avoid excessive dissipation of the waves, C_s should be kept between 0 and 0.5. The default value is 0.0.
- Wave Runup Option (Y/N) The runup scheme used in the numerical model
 is designed to simulate subcritical flow conditions on mild slopes. It cannot
 resolve details of supercritical flow on steep slopes. The runup option should
 only be used with the fully nonlinear model equation option.
- Minimum Flooding Depth Parameter used control the stability of runup computations. Its value should be of the order of one-hundredth of the incident wave height (*H*/100).

Step 9. Output Data

BOUSS-2D calculates the time-dependent evolution of the water-surface elevation and horizontal velocities over a rectangular grid. For most simulations, it would require an excessive amount of disk space to store the surface elevation and velocity data at every grid point for all the simulation time-steps. To minimize disk storage requirements, the program outputs the time-averaged values of the variables over the entire grid or time-histories of the variables at specified grid points in the computational domain. All output files start with a prefix (xxx) specified by the user. The different output file options are given in the following paragraphs:

2-D Spatial Output

• Mean water level $\bar{\eta}(x, y)$ distribution over the computational grid $(xxx_mwl.grd)$ – The free surface fluctuations are averaged over the duration of the synthesized or input time record, t_w , specified in Step 6, i.e.,

$$\overline{\eta}(x,y) = \frac{1}{N} \sum_{t_s-t_w}^{t_s} \eta(x,y,t)$$

where $N = t_w/\Delta t$ and t_s is the duration of the numerical simulation specified in Step 8. The user should make sure that the duration of the numerical simulation is long enough to establish steady-state conditions in the numerical wave basin.

• Significant wave height distribution $H_{\text{mo}}(x,y)$ over the entire computational grid (xxx_Hs.grd) – The significant wave height is calculated as four times standard deviation of the water-surface elevation over the duration of the synthesized or input time record, i.e.,

$$H_{mo}(x,y) = 4\sqrt{\left[\frac{1}{N-1}\sum_{t_s-t_w}^{t_s} \eta^2(x,y,t) - \overline{\eta}^2(x,y)\right]}$$

For regular waves, the wave height can be obtained from the significant wave height as $H_{\rm mo}/\sqrt{2}$. It should noted that there could be differences between the significant wave height estimated from the standard deviation of the time record and those obtained using zero-crossing analysis especially for highly asymmetric waves in shallow water.

• The time-averaged or mean current $\overline{u}_{\alpha}(x,y)$ over the entire computational domain (xxx uv.grd).

$$\overline{\boldsymbol{u}}_{\alpha}(x,y) = \frac{1}{N} \sum_{t,-t_{m}}^{t_{s}} \boldsymbol{u}_{\alpha}(x,y,t)$$

The time-averaging procedure is also carried out over the duration of the synthesized or input time record.

Time Series Output

• Time series of the water-surface elevation $\eta(t)$ and two components of the horizontal velocity $u_{\alpha}(t)$, $v_{\alpha}(t)$ at specified (x,y) locations in the grid. The time series files are named xxx_eta.ts1, xxx u.ts1, and xxx v.ts1.

Animation Output

• Time-dependent output of the water surface elevation $\eta(x,y,t)$ and horizontal velocities $u_{\alpha}(x,y,t)$ over a specified area and time period. The user specifies the coordinates of the lower left-hand corner (x_1,y_1) , upper right-hand corner (x_2,y_2) , and grid skip interval for the output grid area, and the start time, end time, and time-step for the output time period. The files are named xxx.eta and xxx.uv for the surface elevation and velocities, respectively. The animation files could be large and should be used judiciously. The size of the surface elevation output file in bytes can be calculated as 4 x (number of grid points) x (number of time-steps). The velocity file is twice the size of the surface elevation file.

Step 10.

After entering all the information, Pre-BOUSS2D creates a simulation parameter file. The simulation parameter file is an ASCII file that can be edited using

standard text editors (WordPad, etc.). Changes can be made to the wave simulation parameters (e.g., wave height, period, direction, time-step, etc.) and the file saved under a new name. A sample output of the simulation parameter file is shown as follows:

```
barbers_irr_t12.wsp
# BOUSS2D Simulation Parameter File:
# Written By:
                         John. E. Hacker
                         Fri, Sep 15, 2000
# Creation Date:
# Creation Time:
                                 04:16 PM
# Bathymetric Grid Parameters
:BATHY FILE
                       bathy barbers.grd
                       0
                                     # metres
:TIDAL OFFSET
# Damping Parameters
                     damp barbers.grd
:DAMPING FILE
# WaveMaker #1 Parameters
:START WAVEMAKER
                       600
                                     # metres
   WM POS X1
   WM_POS_Y1
                       0
                                     # metres
                                     # metres
   WM_POS_X2
                       600
                       2500
                                     # metres
   WM_POS_Y2
   WAVE TYPE
                 Irreg_uni
                              # Regular, Irreg_uni, or Irreg_multi
   TIME_SERIES_OPTION
                       synthesize
                                     # file or synthesize
                                     # degrees
   WAVE DIRECTION
                       270
                                     # seconds
   TIME_SERIES_DURATION
                       1800
   RANDOM NUMBER SEED
                       25136827
                                 # JONSWAP, BRET, PM, TMA or OCHI
                       JONSWAP
   SPECTRAL TYPE
   JONSWAP OPTION
                       Hs
                                     # Hs, Sigma, or Gamma
                                     # metres
   WAVE HEIGHT SIG
                                     # seconds
   WAVE PERIOD PEAK
                       12
                       8
                                     # seconds
   WAVE PERIOD MIN
                                     # seconds
   WAVE PERIOD MAX
                       24
   GAMMA
                       3.3
                       0.0081
   PHILLIPS
                                    # YES or NO
   RESCALE_SPECTRUM
                       NO
:END WAVEMAKER
```

```
#
# Simulation Parameters
:DURATION
                         2800
                                        # seconds
                         0.2
                                        # seconds
:TIME_STEP
                                         # seconds
:RAMP_DURATION
                         12
:CHEZY_COEFF
                         30
:NONLINEAR_OPTION
                         STRONG
                                        # WEAK or STRONG
:WAVE_RUNUP_OPTION
                         NO
                                        # YES or NO
:WAVE_BREAKING_OPTION
                         YES
                                        # YES or NO
:TURB_LENGTH_SCALE
                         3
                                         # metres
# Output Parameters
:FILE NAME PREFIX
                         irr_h3t12
:HS_FILE
                         irr_h3t12_Hs.r2s # Hs output file
:MEAN_UV_FILE
                         irr_h3t12_mean_UV.r2v # Mean UV output file
# Surface Elevation (ETA) File Parameters
:SAVE ETA
   ETA_FILE
                         irr h3t12.wse
   START TIME
                                        # seconds
   END_TIME
                         1800
                                        # seconds
    SAVE_TIME_STEP
                                        # seconds
                         1
    SAVE FULL GRID
                         YES
                                        # YES or NO
    GRID STEP
                         1
:END SAVE ETA
:SAVE_TIMESERIES
    TS X
                         1220
                                         # metres
                         890
    TS_Y
                                         # metres
: END_TIMESERIES
```

Running BOUSS-2D

After creation of the simulation input file, BOUSS-2D can be run from an MS-DOS command prompt window by typing:

```
C:\BOUSS2D\BIN\bouss2d input_file_name
```

After carrying out computations for 10 time-steps, the program displays an estimate of the run time. The run time could vary, however, depending on other processes running on the computer at the same time.

Time Series Data Analysis

BOUSS-2D outputs the significant wave height and mean current distribution over the entire computational grid. For some applications, it might be necessary to analyze the time series data at specific grid points to obtain frequency or directional wave spectra, wave height statistics, reflection coefficients, etc. Hughes (1993) extensively discusses time and frequency domain analysis techniques for time series data in a laboratory setting. Similar techniques can be applied to time series output from the numerical model.

Standard statistical analysis techniques can be applied to the surface elevation or velocity time records to obtain the mean, standard deviation, skewness, and kurtosis of the time records. The skewness of the surface elevation, η , and its time derivative, η_l , can be used to quantify the degree of wave asymmetry or nonlinearity in shallow water. Zero-crossing analysis techniques can be used to define the heights and periods of individual wave cycles within an irregular wave record. These can be analyzed to obtain parameters such as the root-mean-square wave height, $H_{\rm rms}$, average height of the highest one-third of the waves, $H_{\rm 1/3}$, or the average wave period, $T_{\rm av}$.

Standard spectral analysis techniques can be used to obtain the surface elevation or velocity spectra. These can be analyzed to obtain parameters such as the significant wave height, $H_{\rm mo}$, and spectral peak period, T_p . Different techniques have been proposed for the estimation of directional wave spectra using either an array of wave gauges (e.g., Nwogu 1989) or collocated measurements of the surface elevation and horizontal velocities (e.g., Nwogu et al. 1987). Collocated time series of the surface elevation and horizontal velocities can also be used to estimate the reflection coefficients using the technique described in Hughes (1993).

5 Model Validation

Wave Propagation through a Breakwater Gap

We initially evaluated the ability of BOUSS-2D to simulate the propagation of waves through a gap into a rectangular harbor basin. The basin is 1,200 m wide, 600 m long, and 10 m deep. The width of the opening at the harbor entrance is 120 m.

The first case considered is a regular wave with period T=7 s propagating in a direction normal to the breakwaters. The corresponding ratio of the gap width, B, to wavelength, L, is 2. Boussinesq model simulations were carried out using grid spacings $\Delta x = \Delta y = 3$ m and time-step size $\Delta t = 0.15$ s. A 60-m-wide damping layer was placed around the perimeter of the basin to absorb outgoing waves. Figure 8 shows a snapshot of the instantaneous water-surface elevation produced by the BOUSS-2D model.

The normalized wave height distribution predicted by BOUSS-2D is compared with the numerical solution of Isaacson and Qu (1990) in Figure 9. Isaacson and Qu (1990) used a boundary integral technique to solve the 2-D Helmholtz equation, which is a reduced form of the mild-slope equation for water of constant depth. Good agreement is generally observed between the wave height predictions from the numerical models. Small oscillations can be seen in the Boussinesq model predictions, especially for the smaller wave height contours. This is due to partial wave reflection from the radiation boundaries. Reflection coefficients of the order of 5 to 10 percent at the boundaries have been observed to cause such oscillations in wave height contour lines (Isaacson and Qu 1990)

We next investigated the propagation of irregular multidirectional waves through the gap. The sea state is characterized by a JONSWAP wave spectrum with peak period $T_p = 7$ s and peak enhancement factor $\gamma = 3.3$. A wrappednormal distribution with a standard deviation of 20 deg was used for the directional distribution of wave energy. The double-summation method was used to synthesize time-histories of velocity fluxes along the incident wave boundary for the BOUSS-2D simulations.

Figure 10 shows a snapshot of the instantaneous water-surface elevation produced by the BOUSS-2D model. The normalized wave height distribution predicted by BOUSS-2D is compared with the numerical solution of Isaacson and Qu (1990) in Figure 11. Good agreement is observed. As expected, the

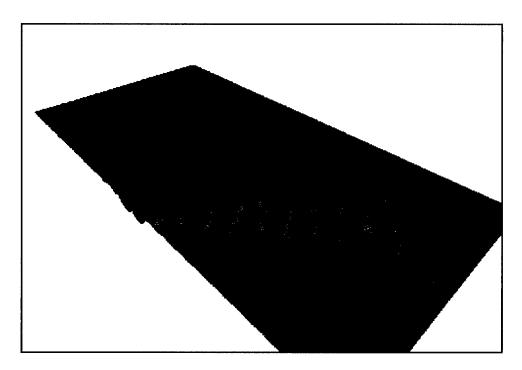


Figure 8. 3-D view of instantaneous water-surface elevation for regular waves propagating through a breakwater gap (T = 7 s, h = 10 m, B/L = 2)

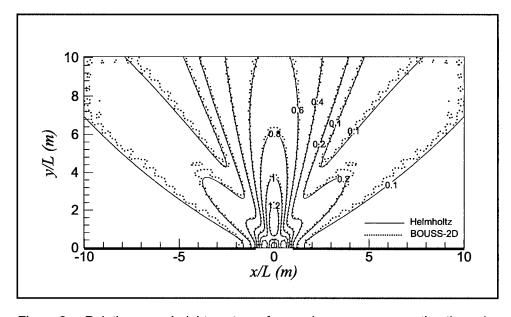


Figure 9. Relative wave height contours for regular waves propagating through a breakwater gap (T = 7 s, h = 10 m, B/L = 2)

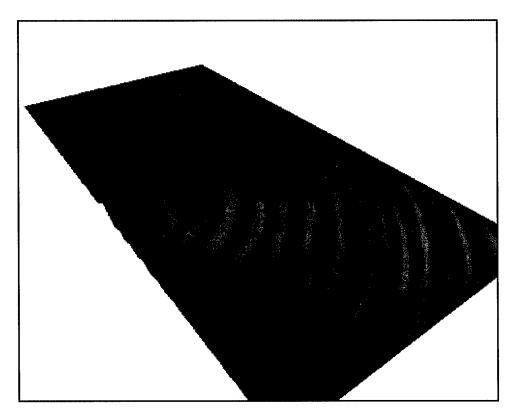


Figure 10. 3-D view of instantaneous water-surface elevation for multidirectional waves propagating through a breakwater gap (T_p = 7 s, σ_θ = 20°, h = 10 m, B/L_p = 2)

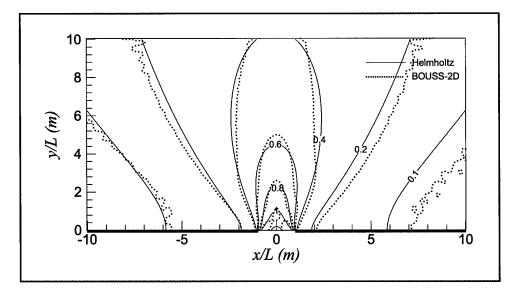


Figure 11. Relative wave height contours for multidirectional waves propagating through a breakwater gap ($T_p = 7 \text{ s}$, $\sigma_\theta = 20^\circ$, h = 10 m, $B/L_p = 2$)

directional spreading of wave energy leads to larger wave heights in the sheltered area behind the breakwaters and smaller wave heights along the principal direction of the waves.

Multidirectional Wave Propagation over a Shoal

Laboratory experiments on the transformation of irregular multidirectional waves over an elliptical shoal were carried out by Vincent and Briggs (1989). The experimental layout is shown in Figure 12, and consists of an elliptical shoal placed in a 0.4572-m-deep basin. The boundary of the shoal is an ellipse defined by:

$$\left(\frac{x - x_c}{3.96}\right)^2 + \left(\frac{y - y_c}{3.05}\right)^2 = 1 \tag{64}$$

where (x_c, y_c) are the coordinates of the center of the shoal and are given by $x_c = 13.72$ m and $y_c = 6.10$ m. The water depth over the shoal is given by:

$$h(x,y) = 0.9144 - 0.7620 \left\{ 1 - \left(\frac{x - x_c}{4.95} \right)^2 - \left(\frac{y - y_c}{3.81} \right)^2 \right\}^{0.5}$$
 (65)

The minimum water depth over the shoal is 0.1524 m. Tests were carried out for various regular and irregular, unidirectional and multidirectional waves. For irregular waves, the TMA spectrum was used to describe the frequency distribution of wave energy, while the wrapped-normal distribution was used for the directional spreading function. Water-surface elevation data were collected at five transects located at distances of 3.05 m, 6.10 m, 9.14 m, 12.19 m, and 15.24 m from the wavemaker as shown in Figure 12.

The numerical basin for the BOUSS-2D model simulations is 31.5 m wide, 27 m long, with a uniform grid spacing of 0.1 m. Two-meter-wide damping layers were placed around the perimeter of the basin to absorb outgoing waves. Two representative test cases were selected for the model-data comparisons. Test case N1 is characterized by a TMA spectrum with significant wave height $H_{\rm mo} = 0.0775$ m, peak period $T_p = 1.3$ s, peak enhancement factor $\gamma = 2$, and a narrow directional distribution with standard deviation $\sigma_{\theta} = 10$ deg. Test case B1 is characterized by a TMA spectrum with significant wave height $H_{\rm mo} = 0.0775$ m, peak period $T_p = 1.3$ s, peak enhancement factor $\gamma = 2$, and a broad directional distribution with standard deviation $\sigma_{\theta} = 30$ deg. Time-histories of the velocity boundary conditions along the wavemaker were synthesized for a duration of 130 s, corresponding to 100 wave periods. Simulations were carried out using a time-step size $\Delta t = 0.025$ s.

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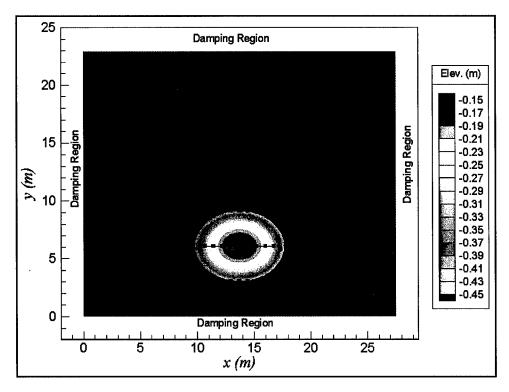


Figure 12. Plan view of bathymetry and layout for Vincent-Briggs shoal experiments

Figure 13 shows a snapshot of the instantaneous water-surface elevation over the shoal predicted by the BOUSS-2D model for test case N1. The focusing of wave energy behind the shoal can clearly be seen. The corresponding 2-D map of the normalized wave height distribution over the computational grid is shown in Figure 14. The predicted wave height variation along transects 3 and 4 are compared to the experimental results in Figures 15 and 16, respectively. BOUSS-2D significantly overpredicted the wave height amplification along transect 3 with differences of the order of 20 to 30 percent. A better match was obtained along transect 4 where the wave height amplification was lower. The reason for such large discrepancies along transect 3 is still unclear. Similar discrepancies were obtained with the CGWAVE model (Demirbilek and Panchang 1998) as shown in Figures 15 and 16. For the broader directional distribution test case B1, reasonable agreement was obtained between the model and the lab data as shown in Figures 17 and 18 with differences of the order of 10 percent.

Wave Breaking in Bimodal Sea States

Bimodal sea states consisting of swell and local wind-generated components occur frequently along most U.S. coastlines (Thompson 1980). Smith and Vincent (1992) investigated the shoaling and breaking of dual-wave systems on a constant slope beach. They found that the higher frequency component decayed much faster in the presence of the low-frequency waves, while the lower frequency component appeared to be unaffected by the presence of high-frequency waves. Smith and Vincent (1992) investigated the applicability of spectral energy

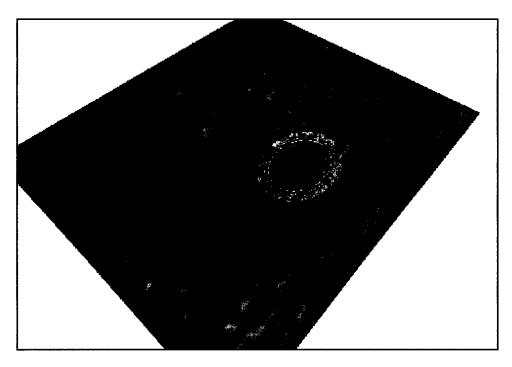


Figure 13. 3-D view of multidirectional wave propagation over a shoal for test case N1 ($H_{\rm mo}$ = 0.0775 m, $T_{\rm p}$ = 1.3 s, $\sigma_{\rm \theta}$ = 10 deg)

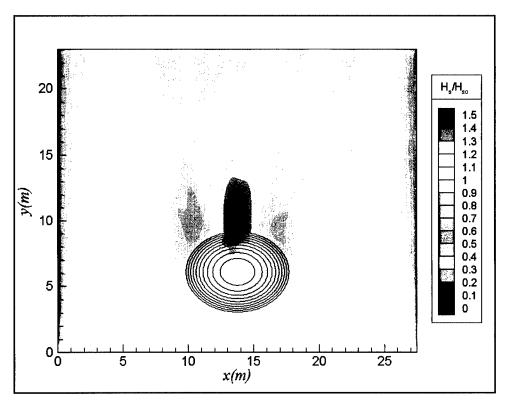


Figure 14. Normalized wave height distribution for multidirectional wave propagation over a shoal for test case N1

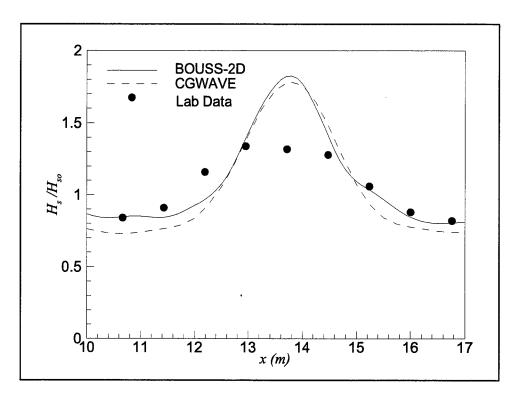


Figure 15. Normalized wave height distribution along transect 3 for test case N1

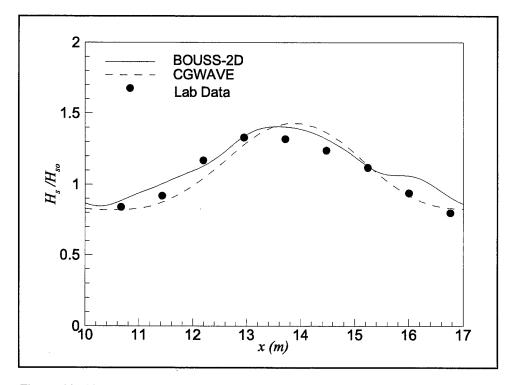


Figure 16. Normalized wave height distribution along transect 4 for test case N1

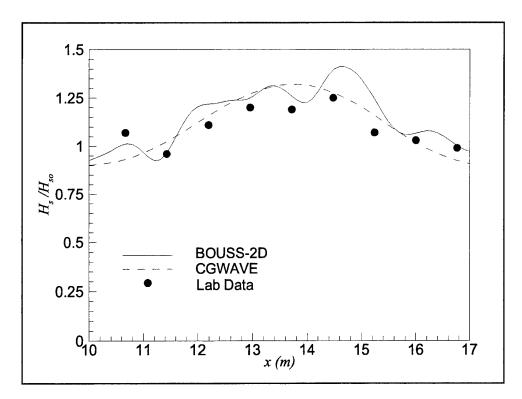


Figure 17. Normalized wave height distribution along transect 3 for test case B1

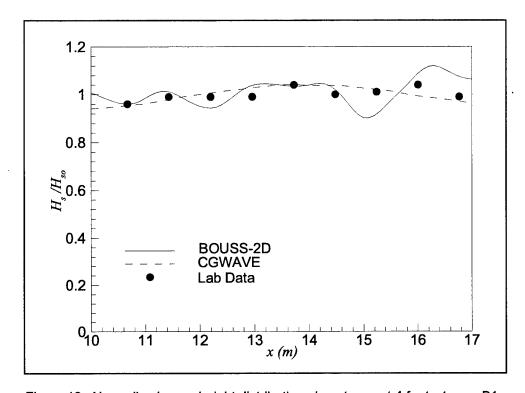


Figure 18. Normalized wave height distribution along transect 4 for test case B1

conservation models with a depth-limited breaking criterion and simpler techniques such as shoaling the component wave systems independently of each other and superimposing the results. None of these techniques could reproduce the observed changes to the wave spectrum.

Boussinesq model simulations were carried out for test case 7 in the Smith and Vincent experiments. The sea state is composed of two irregular wave components described by TMA spectra with $H_{\rm mo,1}=7.6$ cm, $T_{p,1}=2.5$ s, $H_{\rm mo,2}=13.2$ cm, $T_{p,1}=1.75$ s, and $\gamma=20$. The numerical wave flume is 41 m long and consists of a 20-m-long constant-depth region and a 1:30 planar beach. The water depth in the constant depth section of the flume was 0.61 m. The measured time series at the offshore gauge was used to generate velocity boundary conditions for the numerical model. A grid spacing of 0.125 m and time-step size of 0.04 s was used for the numerical simulations.

Figures 19 to 22 show comparisons of the measured and predicted wave spectra at gauges located in water depths of 61 cm, 18.3 cm, 9.1 cm, and 6.1 cm. Although the higher frequency component dominates the incident wave spectrum with 67 percent of the wave energy at h = 61 cm, its energy is preferentially dissipated with the lower frequency component becoming dominant at the shallow depth of 6.1 cm. The Boussinesq model is able to reproduce the observed trends in the experimental data. The primary reason for the preferential reduction in energy of the high-frequency component is due to the nonlinear cross-spectral transfer of energy during the shoaling process.

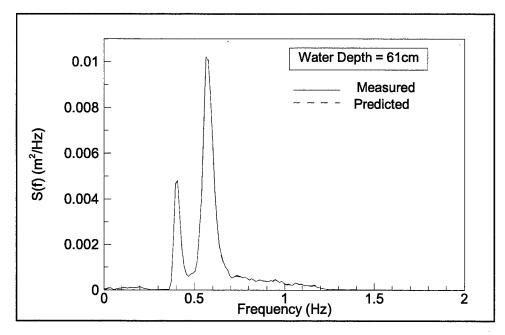


Figure 19. Measured and predicted wave spectra at Gauge 1 for bimodal sea state shoaling on a constant slope beach

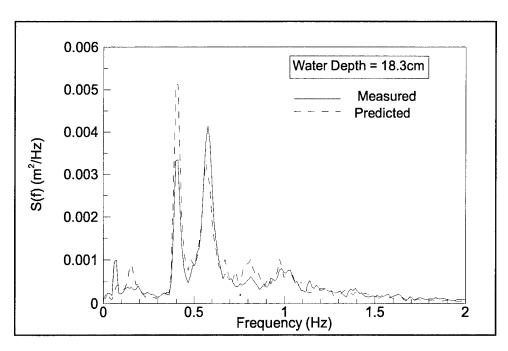


Figure 20. Measured and predicted wave spectra at Gauge 4 for bimodal sea state shoaling on a constant slope beach

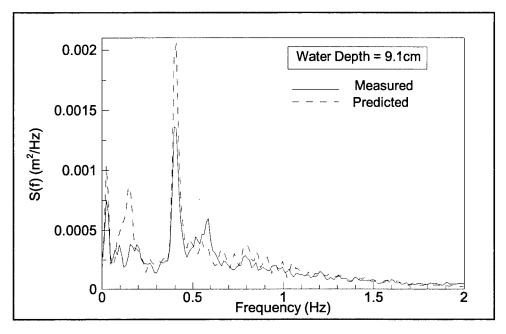


Figure 21. Measured and predicted wave spectra at Gauge 7 for bimodal sea state shoaling on a constant slope beach

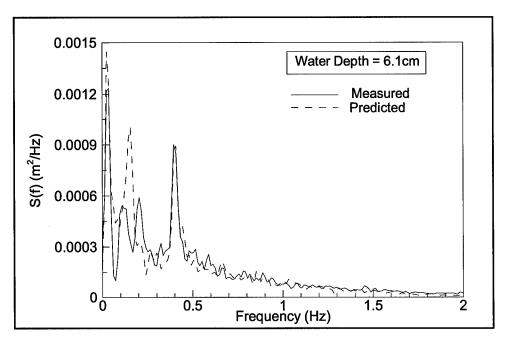


Figure 22. Measured and predicted wave spectra at Gauge 9 for bimodal sea state shoaling on a constant slope beach

Rip Currents on Barred Beaches

Rip currents are narrow, jet-like currents that flow out from the surf zone towards the open ocean. Rip currents are typically generated when there are alongshore variations in the wave breaking location. Alongshore variations could be associated with bathymetric effects (e.g., gaps in sandbars), the presence of structures (piers, jetties, etc.) or edge waves, generated by the trapping of reflected waves near the shoreline. One characteristic feature of rip currents is their unsteady nature. The currents tend to occur episodically as well as oscillate in the horizontal plane (Smith and Largier 1995).

Haller, Dalrymple, and Svendsen (1997) carried out laboratory experiments to investigate the generation of rip currents on a barred beach with rip channels. The bathymetry consists of a 1:30 constant slope beach with a superimposed longshore bar. The bar has two 1.8-m-wide gaps as shown in Figure 23. The water depth is 40 cm at the seaward boundary and 5 cm at the top of the bar. The Boussinesq model was applied to a regular wave test case with height H = 4.5 cm, and period T = 1 s. Numerical simulations were carried out using grid spacings $\Delta x = \Delta y = 0.06$ m and time-step size $\Delta t = 0.015$ s.

Figure 24 shows a snapshot of the instantaneous water-surface elevation 70 s into the simulation. Waves propagating over the bar break on the bar while those propagating through the gap break closer to the shoreline. This sets up a spatial variation of the mean water level and drives a time-varying circulation pattern. Figure 25 shows a 2-D map of the mean currents averaged over 50 wave cycles (from t = 150 s to t = 200 s). As observed in the laboratory experiments, there are two pairs of counterrotating circulation cells. The primary circulation consists of

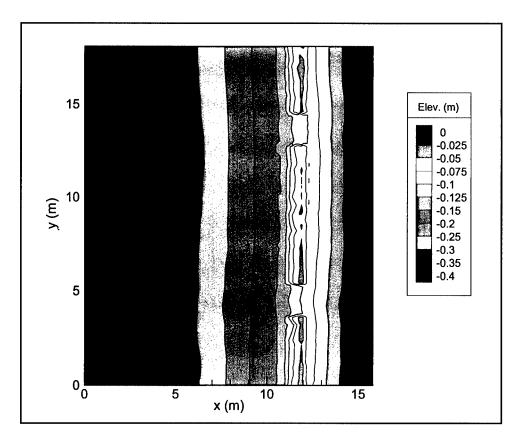


Figure 23. Plan view of bathymetry for rip current experiments

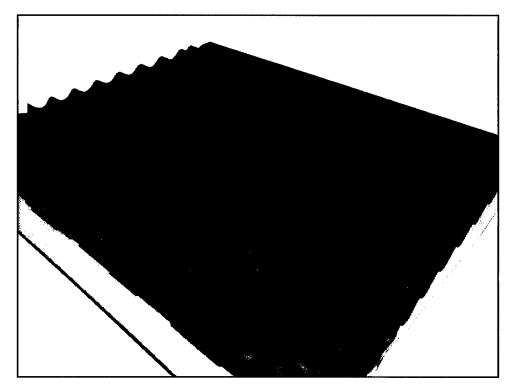


Figure 24. 3-D view of wave propagation over a barred beach with a rip channel (H = 5 cm, T = 1 s)

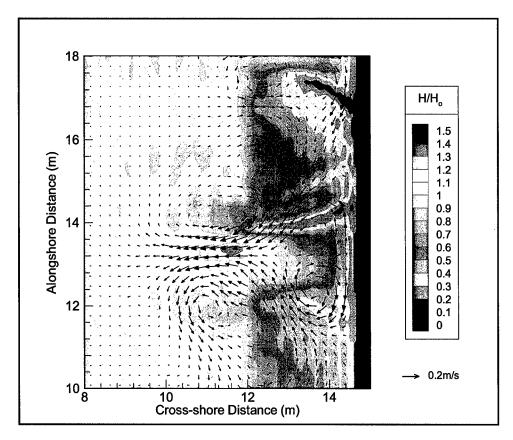


Figure 25. Time-averaged rip current pattern at t = 200 s

opposing longshore currents that converge and flow seawards through the gap in the sandbar. The secondary circulation cell occurs closer to the shoreline.

Wave-Current Interaction

The presence of currents can significantly modify the wave field inside entrance channels and harbors. This is particularly true for adverse currents where the interaction shortens and steepens the waves, leading to potentially hazardous navigation conditions. Smith et al. (1998) carried out laboratory experiments to investigate wave-current interaction in an idealized inlet. The bathymetry and layout used for the numerical simulations is shown in Figure 26. The wave basin is 24 m wide and 18.25 m long. The water depth variation adjacent to the inlet is given by the equilibrium beach profile:

$$h = 0.036y^{0.67} + 0.022 (66)$$

The equilibrium profile extends to a water depth of 0.205 m beyond which it is linearly transitioned at a slope of 1:7 to the constant depth region of 0.325 m. The entrance channel is lined by two parallel jetties that extend a distance of 3.8 m from the shoreline (y = 0) with an entrance width of 4 m.

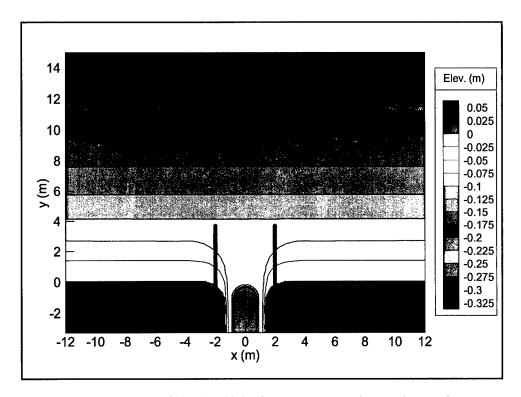


Figure 26. Bathymetry of idealized inlet for wave-current interaction study

A 2-D hydrodynamic model was run to provide the current field for use in the wave model simulations. Figure 27 shows a map of the current field generated by the model. Boussinesq model simulations were carried out using grid spacings $\Delta x = \Delta y = 0.075$ m and time-step size $\Delta t = 0.015$ s. The incident wave conditions were characterized by a TMA spectrum with $H_{mo} = 0.055$ m, $T_p = 1.4$ s, and $\gamma = 3.3$. The predicted wave height distributions for current speeds U = 0 m/s and U = 0.24 m/s are shown in Figures 28 and 29, respectively. The Boussinesq model predicted an increase of 15 to 20 percent in the significant wave height near the entrance channel. The laboratory measurements, however, showed a slight decrease in wave height through the channel due to the effect of wave breaking. A more detailed investigation of the wave-breaking criterion and energy dissipation rates in the presence of currents will be carried out to improve simulations of wave-current interaction in the Boussinesq model.

Wave Transformation Near Ponce de Leon Inlet, Florida

Ponce de Leon Inlet, an inlet leading into the Halifax and Indian Rivers in Florida has a complex bathymetry featuring a large ebb shoal, a navigation channel, and a jetty. A 1:100 laboratory model study of a 4.2-km by 1.4-km region near the inlet was carried out at the U.S. Army Engineer Research and Development Center (ERDC) Coastal and Hydraulics Laboratory (CHL). Tests were conducted for sea states with different wave heights, peak periods, spectral widths, and directional spread. The TMA spectrum was used to describe the frequency distribution of wave energy, while the wrapped-normal distribution

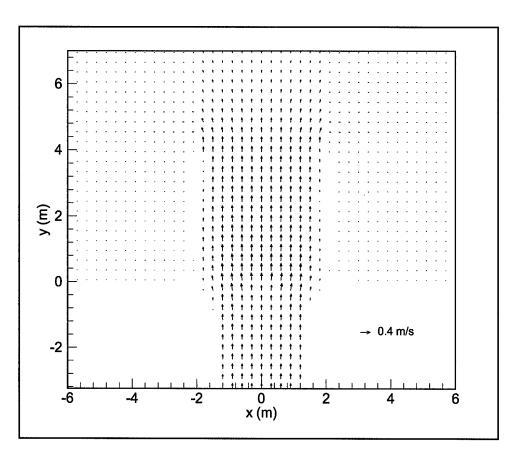


Figure 27. Predicted current field for U = 0.24 m/s

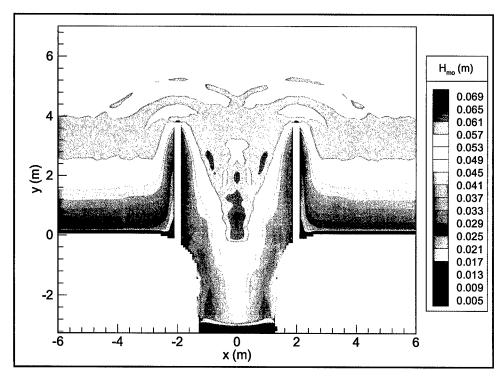


Figure 28. Predicted wave height distribution near inlet for test case without currents ($H_{\rm mo}$ = 0.055 m, $T_{\rm p}$ = 1.4 s, U = 0 m/s)

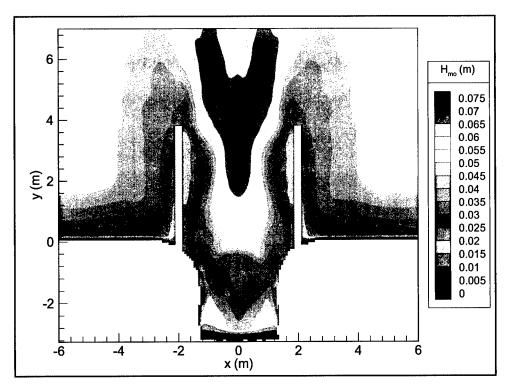


Figure 29. Predicted wave height distribution near inlet for test case with currents ($H_{mo} = 0.055 \text{m}$, $T_p = 1.4 \text{ s}$, U = 0.24 m/s)

was used for the directional spreading function. Water-surface elevation data were recorded at 30 locations.

BOUSS-2D was run for one of the multidirectional test cases characterized by $H_{\text{mo}} = 0.95$ m, $T_p = 10$ s, $\gamma = 5$, and directional spread $\sigma_{\theta} = 20$ deg (Test No. 11). The bathymetry used for the numerical simulations is shown in Figure 30. Boussinesq model simulations were carried out using $\Delta x = \Delta y = 5$ m and $\Delta t = 0.15$ s. Time-histories of the velocity boundary conditions along the wave-maker were synthesized using the double-summation method for a duration of 500 s, corresponding to 50 wave periods.

A snapshot of the instantaneous water-surface elevation produced by the BOUSS-2D model is shown in Figure 31. The corresponding significant wave height distribution is shown in Figure 32. Two distinct wave-focusing regions can be observed on the shoal. The predicted wave height variations along the offshore and nearshore gauge arrays are compared to the experimental results in Figures 33 and 34, respectively. BOUSS-2D reasonably reproduced the wave height variation along the offshore array, although differences of the order of 20 percent exist at a couple of gauge locations. For the nearshore array, excellent agreement is obtained between BOUSS-2D model predictions and the experimental data.

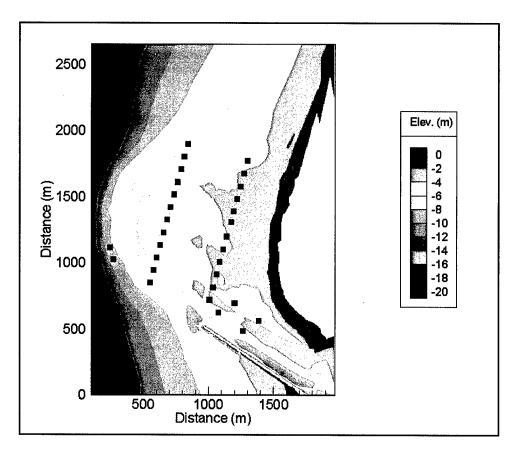


Figure 30. Ponce de Leon Inlet model bathymetry

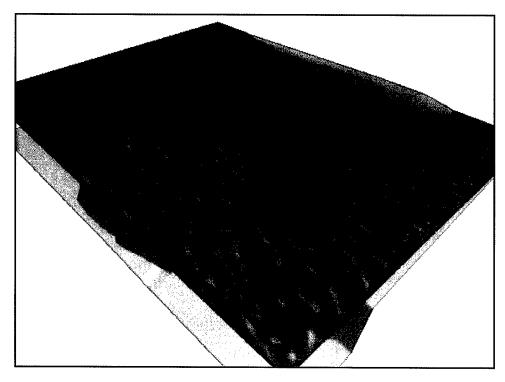


Figure 31. 3-D view of multidirectional wave propagation near Ponce de Leon Inlet ($H_{\rm mo}$ = 0.95 m, T_{p} = 10 s, σ_{θ} = 20 deg)

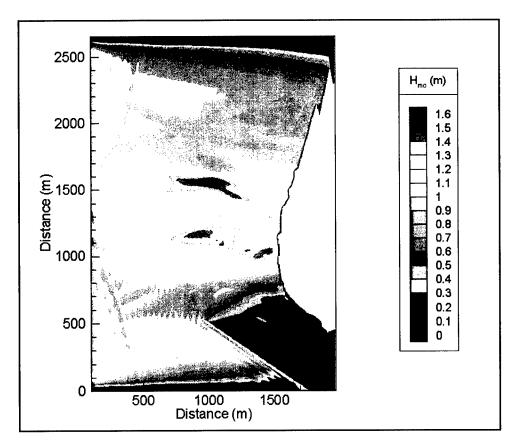


Figure 32. 2-D map of wave height distribution predicted by Boussinesq model ($H_{\rm mo}$ = 0.95 m, $T_{\rm p}$ = 10 s, $\sigma_{\rm \theta}$ = 20 deg)

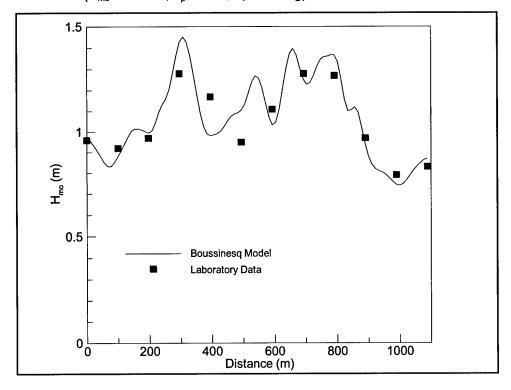


Figure 33. Measured and predicted wave height distribution along the offshore gauge array ($H_{\rm mo}$ = 0.95 m, T_{ρ} = 10 s, σ_{θ} = 20 deg)

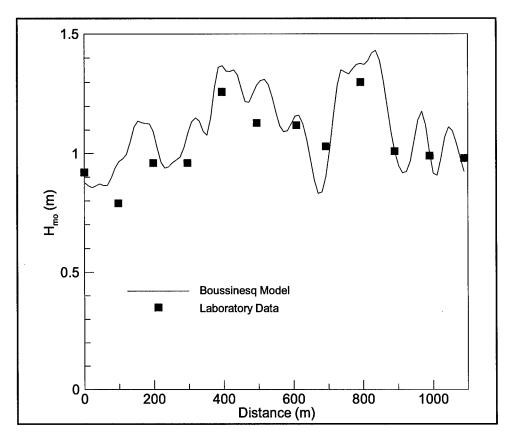


Figure 34. Measured and predicted wave height distribution along the nearshore gauge array ($H_{\text{mo}} = 0.95 \text{ m}$, $T_{p} = 10 \text{ s}$, $\sigma_{\theta} = 20 \text{ deg}$)

Wave Disturbance in Barbers Point Harbor, Hawaii

Barbers Point Harbor is a small harbor in Hawaii that has experienced occasional long-period harbor oscillation problems. The main harbor basin is 11.6 m deep, and is connected to the Pacific Ocean through a 12.8-m-deep, 1.3-km-long entrance channel. The water depths are shallow (2 to 10 m) in the vicinity of the entrance channel, leading to the nonlinear generation of free and forced long-period waves near the harbor entrance. Free long waves could be resonantly amplified inside the harbor basin if the long-wave periods are close to any of the natural modes of oscillation of the basin.

BOUSS-2D was used to investigate to the resonant harbor oscillation periods and the wave height amplification factors. A three-dimensional view of the bathymetry and harbor layout used for the simulations is shown in Figure 35. The offshore boundary was truncated at a water depth of 50 m. Numerical simulations were carried for regular waves with periods ranging from 50 s to 200 s. Wave height information was output at two gauges outside the harbor and four gauges inside the harbor as shown in Figure 36.

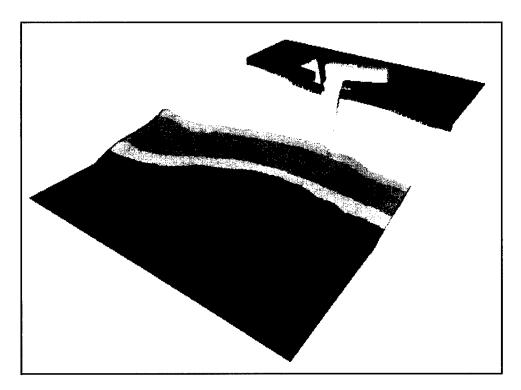


Figure 35. 3-D view of Barbers Point Harbor model bathymetry

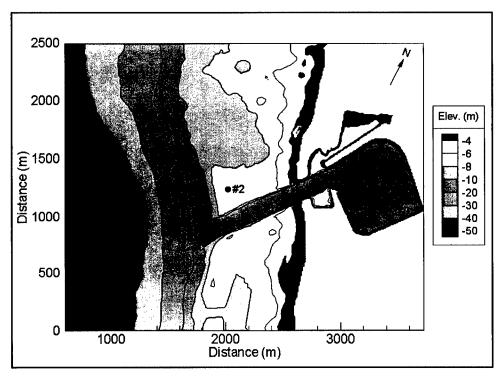


Figure 36. 2-D map of Barbers Point Harbor bathymetry showing wave gauge locations

The predicted wave heights at two gauge locations inside the basin, normalized by the incident wave height, are compared with predictions from the elliptic mild-slope model CGWAVE (Demirbilek and Panchang 1998) in Figures 37 and 38. The harbor exhibits a number of distinct periods of oscillation (60 s, 83 s, 110 s, 130 s, 143 s, and 190 s). The Helmholtz or pumping mode of the basin occurs at a period of around 900 s. Good agreement is generally observed between wave height amplification factors predicted by both models. It should be pointed out that it takes longer to attain steady-state conditions in time-domain models, especially for resonant oscillations. Figure 39 shows a plot of the time history at Gauge 5 for one of the resonance periods (T = 60 s). Steady-state conditions are attained approximately 30 wave periods after the waves initially arrived at the gauge location.

Although linear, frequency-domain models are computationally more efficient at predicting harbor resonance periods and amplification factors, they cannot predict the magnitude of the long-period wave energy inside a harbor from a given offshore wind-wave spectrum. To overcome this deficiency, Okihiro, Guza, and Seymour (1993) used an ad-hoc coupling of a nonlinear model for the generation of bound long waves outside a harbor with a linear model for the amplification of long waves inside the harbor. The complex nature of bathymetry outside Barbers Point Harbor makes it difficult to quantify the relative amount of long-wave energy outside the harbor that is freely propagating into the harbor. The entrance channel is much deeper than the surrounding areas. Free long waves would be generated along the steep side slopes of the entrance channel as well as reflected from shoreline. The long waves would thus be propagating over a wide range of directions.

We investigated the ability of the Boussinesq model to simultaneously model the nonlinear generation of long waves by storm waves propagating from deep to shallow water, the diffraction of both short and long period waves into the harbor basin, and the resonant amplification of long waves inside a harbor. We initially considered a bichromatic wave train with component periods $T_1 = 12$ s, $T_2 =$ 13.46 s, and heights $H_1 = H_2 = 1.5$ m. The group period of 110 s corresponds to one of the natural periods of oscillation of the basin. Numerical simulations were carried out with $\Delta x = \Delta y = 10$ m and $\Delta t = 0.2$ s. The simulated surface elevation time-histories at the offshore Gauge 1, harbor entrance Gauge 2, and harbor basin Gauges 3 and 5 are shown in Figure 40. The long-period component, obtained by applying a low-pass filter (T > 25 s), is also shown in the figures. It can be seen that nonlinear interactions during the shoaling process lead to an amplification of the long-period wave component between the offshore Gauge 1 which is in 50 m of water, and the harbor entrance Gauge 2 which is 7 m of water. Inside the harbor basin, the long waves are further amplified and dominate the harbor response at Gauge 5.

Although bichromatic waves are useful for demonstrating the importance of nonlinear wave-wave interactions in harbor response, natural sea states are irregular with wave energy distributed over a large number of frequency components. We simulated the response of the harbor to an irregular wave train. Numerical simulations were carried out for an incident sea state characterized by a JONSWAP spectrum with $H_{\text{mo}} = 3$ m, $T_p = 12$ s and $\gamma = 3.3$. Figure 41 shows a

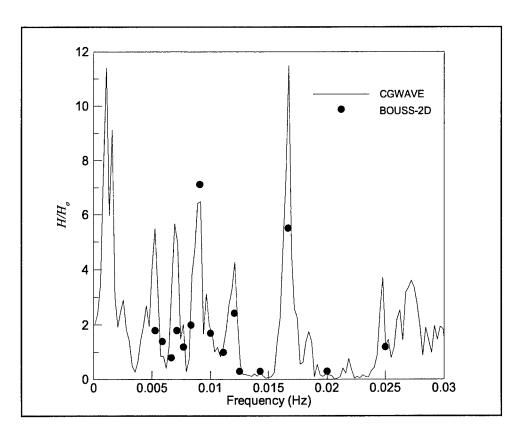


Figure 37. CGWAVE and BOUSS-2D model predictions of the wave height amplification factor at Gauge 5

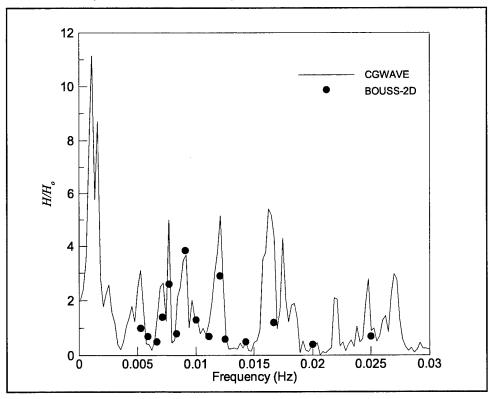


Figure 38. CGWAVE and BOUSS-2D model predictions of the wave height amplification factor at Gauge 6

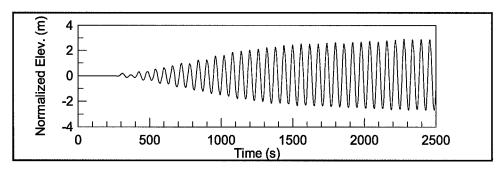


Figure 39. Boussinesq model prediction of the time-history of the water-surface elevation at Gauge 5 for a natural harbor period (T = 60 s)

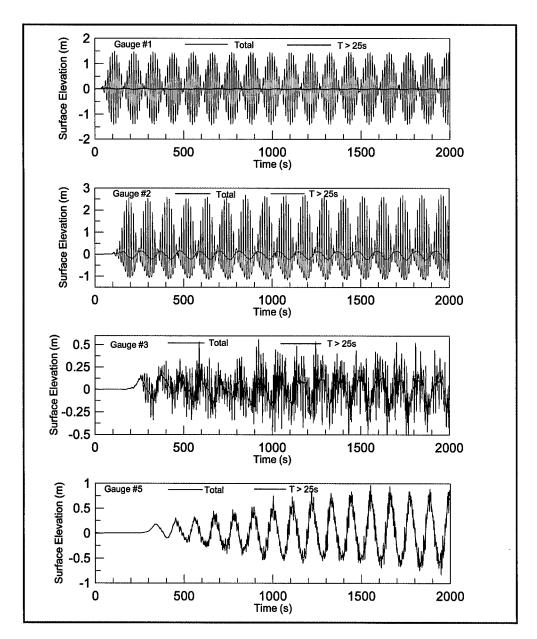


Figure 40. Time-histories of total and long-period (T > 25 s) component of watersurface elevation at Gauges 1, 2, 3, and 5 for bichromatic wave train

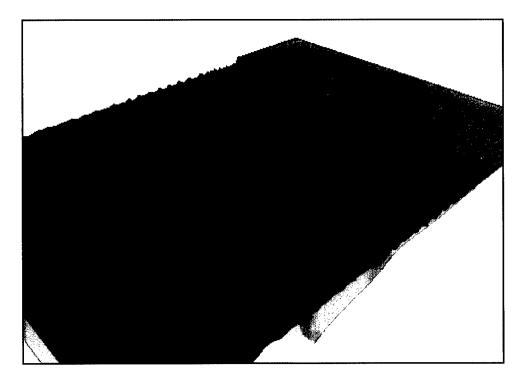


Figure 41. 3-D view of irregular wave propagation into Barbers Point Harbor

snapshot of waves propagating into the harbor. The predicted wave spectra at Gauges 1 and 2 are shown in Figure 42. It can be seen that nonlinear interactions significantly modified the wave spectrum at Gauge 2 (h = 7 m), with the cross-spectral transfer of energy to both lower and higher harmonics. The wave spectra for the four gauges located inside the harbor basin are plotted in Figure 43. The short-period wave energy is much smaller inside the harbor basin because the bathymetry acts to refract waves away from the harbor entrance.

The wave spectra were divided into short-period (T < 25 s) and long-period components (T > 25 s) and wave heights were calculated for each component. The short-period wave heights at the inside gauges varied from 0.42 to 0.57 m, compared to 3.1 m at outside Gauge 2. The long-wave energy inside the harbor is, however, comparable to that at the outside gauge with heights ranging from 0.38 to 0.46 m for the inside gauges, compared to 0.49 m at an outside Gauge 2.

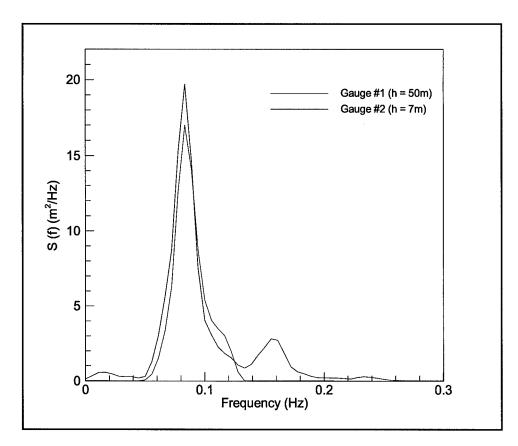


Figure 42. Predicted wave spectra at the outside Gauges 1 and 2 for an irregular sea state ($H_{\rm mo}$ = 3 m, $T_{\rm p}$ = 12 s)

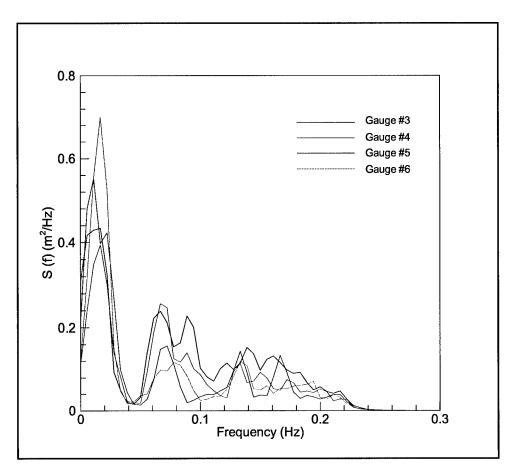


Figure 43. Predicted wave spectra at gauges inside harbor basin (Gauges 3-6) for an irregular sea state ($H_{\rm mo}$ = 3 m, T_p = 12 s)

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Appendix A Fourier Series Solutions of Boussinesq Equations

As the height of surface waves in intermediate and shallow-water depths increases, the wave profile changes from a sinusoidal shape to an asymmetric one with peaked crests and broad shallow troughs. The Boussinesq equations are nonlinear and are able to describe the change in wave shape, provided the wave height and period are within nonlinear and dispersive limits of the equations. However, it is important that the velocity and flux time-histories imposed along the wave generation boundaries of the numerical model be consistent with the equations that are solved within the computational domain. In BOUSS-2D, the Fourier approximation method of Rienecker and Fenton (1981)¹ has been used to derive nonlinear boundary conditions for periodic waves in water of constant depth. The one-dimensional form of the weakly nonlinear form of the Boussinesq equations (Equations 4 to 6) for water of constant depth can be written as:

$$\eta_t + \left[(h + \eta) u_\alpha \right]_x + \left(\alpha + \frac{1}{3} \right) h^3 u_{\alpha, x c x} = 0$$
 (A1)

$$u_{\alpha,t} + g\eta_x + \frac{1}{2} (u_\alpha^2)_x + \alpha h^2 u_{\alpha,xxt} = 0$$
 (A2)

For periodic waves, the partial differential equations can be transformed into a set of coupled nonlinear ordinary differential equations in terms of coordinate system, $\xi = x - Ct$, moving at the phase speed of the waves, C, and integrated once to yield:

$$(h+\eta)u_{\alpha} + \left(\alpha + \frac{1}{3}\right)h^3u_{\alpha,\xi\xi} + Q = 0 \tag{A3}$$

$$g\eta + \frac{1}{2} \left(u_{\alpha}^{2} \right) + \alpha h^{2} u_{\alpha,\xi\xi} - R = 0 \tag{A4}$$

References cited in Appendices A-E are listed in the References at the end of the main text.

where Q is the volume flux and R is the Bernoulli constant. The velocity u_{α} can be expanded as a Fourier series:

$$u_{\alpha} = B_0 + \sum_{j=1}^{N} jkB_j \cos(jk\xi) \tag{A5}$$

where N is the number of Fourier components, B_j are the Fourier coefficients, and k is the wave number. To solve the problem numerically, the free surface elevation is discretized into N+1 equally spaced points over half a wavelength, i.e.,

$$\eta_m = \eta(\xi_m), m = 0, 1, \dots, N \tag{A6}$$

where $\xi_m = mL/2N$ and L is the wavelength. Equations A3 to A4 are then evaluated at points over half a wavelength to yield a system of nonlinear algebraic equations:

$$(h + \eta_m)u_m + \left(\alpha + \frac{1}{3}\right)h^3 u_{\xi\xi,m} + Q = 0$$
 (A7)

$$g\eta_m + \frac{1}{2}u_m^2 + \alpha h^2 u_{\xi\xi,m} - R = 0$$
 (A8)

The above 2N+2 equations involve 2N+5 unknowns η_j (j=0,...,N), B_j (j=0,...,N), k, Q, R, so three additional equations are needed. These can be obtained from the wave height, H, wave period, T, the mean water level as:

$$\eta_0 - \eta_N - H = 0 \tag{A9}$$

$$kCT - 2\pi = 0 (A10)$$

$$\eta_0 + \eta_N + 2 \sum_{j=1}^{N-1} \eta_j = 0 \tag{A11}$$

noting that $C = -B_0$ for a zero-mean Eulerian velocity. A Newton-Raphson procedure (see Rienecker and Fenton 1981) is used to solve the system of equations (A7 to A11) for the unknown values of the free surface displacement at the collocation points, the Fourier coefficients, the wave number, the phase speed, and the constants Q and R.

Appendix B Description of Ocean Wave Spectra

A number of parametric shapes have been proposed to describe the frequency distribution of wave energy. The spectral shapes were derived from long-term field wave measurements and depend on factors such as wind duration, the distance or fetch over which the wind blows, and water depth.

Pierson-Moskowitz Spectrum

For fully-developed sea states in deep water where there is a local balance between momentum transfer from the wind and wave breaking/nonlinear cross-spectral energy transfer processes, Pierson-Moskowitz (1964)¹ proposed the following wave spectrum:

$$S(f) = \frac{\alpha g^2}{(2\pi)^4 f^5} \exp\left[-\beta \left(\frac{f}{f_p}\right)^{-4}\right]$$
 (B1)

where $\alpha = 0.0081$ is Phillips' constant, g is the gravitational acceleration, $\beta = 0.74$, $f_p = g/2\pi U_{19.5}$, and $U_{19.5}$ is the wind speed at 19.5 m above the mean sea level.

Bretschneider Spectrum

The Bretschneider spectrum (Bretschneider 1959) has the same shape as the Pierson-Moskowitz spectrum but is defined in terms of the significant wave height, H_s , and spectral peak frequency, f_p , instead of the wind speed. It can be written as:

References cited in this appendix are listed in the References at the end of the main text.

$$S(f) = \frac{5H_s^2}{16} \frac{1}{(f/f_p)^5} \exp\left[-\frac{5}{4} \left(\frac{f}{f_p}\right)^4\right]$$
 (B2)

JONSWAP Spectrum

Based on an extensive analysis of data from the Joint North Sea Wave Observation Project (JONSWAP), Hasselmann et al. (1973) proposed the following modified form of the Pierson-Moskowitz spectrum to account for fetch-limited conditions:

$$S(f) = \frac{\alpha g^2}{(2\pi)^4 f^5} \exp\left[-\frac{5}{4} \left(\frac{f}{f_p}\right)^{-4}\right] \gamma^a$$
 (B3)

where

$$\alpha = 0.076 \left(\frac{U_{10}^2}{gF} \right)^{0.22} \tag{B4}$$

$$f_p = 3.5 \left(\frac{U_{10}^2}{gF}\right)^{1/3} \tag{B5}$$

$$a = \exp\left[-(f - f_p)^2 / 2\sigma^2 f_p^2\right]$$
 (B6)

$$\begin{cases} \sigma_a = 0.07 & \text{for } f < f_p \\ \sigma_b = 0.09 & \text{for } f < f_p \end{cases}$$
 (B7)

F is the fetch distance, γ is a spectral peak enhancement factor, and U_{10} is the wind speed at 10 m above the mean sea level. Figure B1 shows a comparison of a JONSWAP spectrum with $\gamma = 3.3$ with a Bretschneider spectrum for a sea state. The JONSWAP spectrum reduces to the Bretschneider spectrum when γ is equal to 1.0.

TMA Spectrum

The TMA spectrum is a modified version of the JONSWAP spectrum for water of finite depth. It was proposed by Bouws, Gunther, and Vincent (1985) based on Kitaigorodskii, Krasitskii, and Zaslavskii (1975) frequency-dependent factor for the equilibrium range of the wave spectrum in shallow-water and validated with data from three field studies (Texel, MARSEN, and ARSLOE). It can be written as:

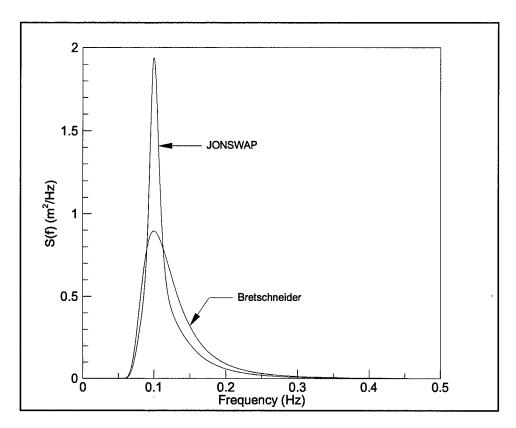


Figure B1. Comparison of Bretschneider and JONSWAP (γ = 3.3) spectra for a sea state with $H_{\rm mo}$ = 1 m, T_p = 10 s

$$S(f) = \frac{\alpha g^2}{(2\pi)^4 f^5} \exp\left[-\frac{5}{4} \left(\frac{f}{f_p}\right)^{-4}\right] \gamma^a \cdot \lambda(f, h)$$
 (B8)

where $\lambda(f,h)$ is a function that expresses the effect of finite water depth and is given by:

$$\lambda(f,h) = \left[R(\omega_h)\right]^{-2} \left\{1 + \frac{2\omega_h^2 R(\omega_h)}{\sinh[2\omega_h^2 R(\omega_h)]\left[2\omega_h^2 R(\omega_h)\right]}\right\}^{-1}$$
(B9)

The frequency factor $\omega_h = 2\pi f \sqrt{(h/g)}$ and $R(\omega_h)$ is obtained from the iterative solution of the linear dispersion relation:

$$R(\omega_h) \tanh \left[\omega_h^2 R(\omega_h) \right] = 1$$
 (B10)

Ochi-Hubble Spectrum

The Ochi-Hubble spectrum (Ochi and Hubble 1976) is a six-parameter spectrum proposed for bimodal sea states consisting of swell and local windgenerated components. It can be written as:

$$S(f) = \frac{\pi}{2} \frac{\left[(4\gamma_1 + 1)(2\pi f_{p_1})^4 / 4 \right]^{\gamma_1}}{\Gamma(\gamma_1) (2\pi f)^{4\gamma_1 + 1}} H_{s_1}^2 \exp\left[-\frac{4\gamma_1 + 1}{4} \left(\frac{f}{f_{p_1}} \right)^{-4} \right] + \frac{\pi}{2} \frac{\left[(4\gamma_2 + 1)(2\pi f_{p_2})^4 / 4 \right]^{\gamma_2}}{\Gamma(\gamma_2) (2\pi f)^{4\gamma_2 + 1}} H_{s_2}^2 \exp\left[-\frac{4\gamma_2 + 1}{4} \left(\frac{f}{f_{p_2}} \right)^{-4} \right]$$
(B11)

where Γ is the gamma function. H_s , f_p , and γ denote the significant wave height, spectral peak frequency, and spectral shape factor respectively for the two sea state components. When γ is equal to 1, the Ochi-Hubble spectrum reduces to the Bretschneider spectrum.

Appendix C Directional Wave Spreading Functions

The directional spreading function, $D(\theta)$, describes the directional distribution of wave energy in irregular multidirectional sea states. It can be quantified in terms of the principal direction of wave propagation θ_p , and the directional spread or standard deviation of the spreading function, σ_{θ} , which is defined as:

$$\sigma_{\theta}^{2} = \int_{\theta_{p}-\pi/2}^{\theta_{p}+\pi/2} D(\theta) (\theta - \theta_{p})^{2} d\theta$$
 (C1)

A number of parametric shapes have been proposed to describe the directional spreading function including the cosine-power, the circular normal, and wrapped-normal distributions. These are described in the following paragraphs.

Cosine-Power Spreading Function

The cosine-power function is an extended version of the cosine-squared directional distribution initially proposed by St. Denis and Pierson (1953)¹ and can be written as:

$$D(\theta) = \frac{\Gamma(s+1)}{\sqrt{\pi} \Gamma(s+1/2)} \cos^{2s}(\theta - \theta_p) \qquad \text{for } |\theta - \theta_p| < \pi/2$$
 (C2)

where Γ is the gamma function. The parameter s is an index describing the degree of directional spreading with $s \to \infty$ representing a unidirectional wave field.

Circular-Normal Spreading Function

The circular normal distribution was proposed by Borgman (1969) and can be written as:

References cited in this appendix are listed in the References at the end of the main text.

$$D(\theta) = \frac{1}{2\pi I_0(a)} \exp\left[a\cos(\theta - \theta_p)\right]$$
 (C3)

where I_0 is the modified Bessel function of the first kind and a is a parameter describing the degree of directional spreading with $a \to \infty$ representing a unidirectional wave field.

Wrapped-Normal Spreading Function

The wrapped-normal distribution was suggested by Mardia (1972) and is given by:

$$D(\theta) = \frac{1}{2\pi} + \frac{1}{\pi} \sum_{i=1}^{N} \exp\left[-\frac{1}{2} (j\sigma_{\theta})^{2}\right] \cos\left[j(\theta - \theta_{p})\right]$$
 (C4)

Figure C1 shows a plot of the distributions for the three different spreading function formulations corresponding to a standard deviation σ_{θ} of 25.5 deg. The associated spreading indices are s=2 for the cosine-power function and a=5.55 for the circular-normal distribution. Thirty components (N=30) were used for the wrapped-normal distribution. The cosine-normal and wrapped-normal distributions are slightly narrower than the cosine-power function although the differences can be considered to be minimal.

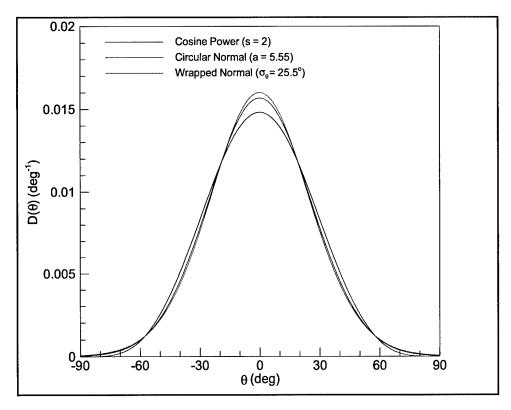


Figure C1. Comparison of the cosine-power, circular-normal and wrapped-normal distributions with a standard deviation of 25.5 deg

Appendix D BOUSS-2D File Formats

BOUSS-2D currently supports two file formats. The grid format (.grd) is used to define the spatial variation of scalar or vector quantities over a rectangular grid. The time series format (.ts1) is used for one-dimensional time-histories of scalar quantities. The files consist of a header section and a data section. The header section includes both mandatory parameters required to define the data structure and optional parameters that provide additional information on the data. Comment lines in the header section begin with the pound (#) sign, and lines with parameter names and values begin with the colon (:) sign.

Grid File Format (.grd)

The grid file format is used to store multiple 2-D arrays $h_1(x,y)$, $h_2(x,y)$, etc. The variables are defined over a rectangular grid with the origin located at $(x_{\text{origin}}, y_{\text{origin}})$ and uniform grid spacings Δx and Δy in the x and y directions respectively. The number of grid points are N_x and N_y in the x and y directions respectively. The 2-D array h(i,j) represents the value of h(x,y) at $x = x_{\text{origin}} + (i-1)\Delta x$ and $y = y_{\text{origin}} + (j-1)\Delta y$. The mandatory header parameters are:

- NGrid X = number of grid points in the x direction (N_x)
- NGrid_Y = number of grid points in the y direction (N_v)
- Delta $X = grid spacing in the x direction (<math>\Delta x$)
- Delta Y = grid spacing in the y direction (Δy)
- X Origin = x-coordinate of grid origin
- Y Origin = y-coordinate of grid origin
- N_Arrays = number of data arrays (1 for scalar quantities, 2 for vector quantities)

The header section must terminate with the *EndHeader* keyword. Two-dimensional data are then written out after the header section as continuous data streams in row first order, i.e., $((h(i,j), i = 1, N_x), j = 1, N_y)$ for scalar quantities or $((u(i,j), i = 1, N_x), j = 1, N_y)$ and $((v(i,j), i = 1, N_x), j = 1, N_y)$ for vector quantities. A sample grid file is provided as follows:

```
# BOUSS2D Grid File
:FileName bathy.grd
:WrittenBy Bouss2D Version 1.0
:CreationDate Mon Sep 18 12:40:25 2000
:N_Arrays
:DataDescription(1) Seabed Elevation
:DataUnits(1)
                  meters
:NGrid X
              4
:NGrid Y
              4
:Delta_X
              10.0
:Delta Y
             10.0
:X Origin
             0.0
:Y Origin
              0.0
:EndHeader
```

Time Series File Format (.ts1)

The time series file format is used to store time-histories of scalar quantities u(t) at discrete time intervals $t_i = t_1 + (i-1)\Delta t$, where t_1 is the start time and Δt is the time-step. The number of data points in the time record is N_t . Multiple time-histories (e.g., data output at different grid locations) can be stored in the same file. The mandatory header parameters are:

- NTimeSteps = number of time-steps (N_t)
- TimeStep = time-step (Δt)
- StartTime = start time of record (s)
- NDatasets = number of time series records

The header section terminates with the *EndHeader* keyword. Data are then written out after the header section as a single column vector for one time record or multiple columns for multiple time records. A sample time series file is provided as follows:

```
# BOUSS2D Time Series File
:FileName test.tsl
:WrittenBy Bouss2D
                    Bouss2D Version 1.0
:CreationDate Mon Sep 18 12:40:25 2000
:NDataSets
:DataDescription(1) Surface Elevation
                            meters
:DataUnits(1)
:DataDescription(2) Surface Elevation
:DataUnits(2) meters
:DataDescription(3) Surface Elevation
:DataUnits(3)
:DataUnits(3)
:DataDescription(4)
:DataInits(4)

:DataInits(4)

:DataInits(4)

:DataUnits(3)

:DataUnits(3)

:DataUnits(3)

:Medell

Surface Elevation

meters
                              meters
:StartTime
                              0.0000
:TimeStep
                               0.1500
:NTimeSteps
                               5334
```

```
270.0000
1030.0000
500.0000
1030.0000
820.0000
1030.0000
1000.0000
:x grid(1)
____(1)
:y_grid(1)
:x_grid(2)
:y_grid(2)
:x_grid(3)
:y_grid(3)
x grid(4)
:y_grid(4)
:EndHeader
    0.000000E+00 -1.772061E-15 -1.234493E-14 -4.485098E-14 -1.195287E-13 -2.679531E-13 -5.388106E-13 -1.005685E-12
    -1.777521E-12 -3.012488E-12 -4.936255E-12 -7.866251E-12
    -1.224317E-11 -1.867146E-11 -2.797059E-11 -4.124122E-11
    -5.994772E-11 -8.602132E-11 -1.219879E-10 -1.711262E-10
   -2.376610E-10 -3.269985E-10 -4.460105E-10 -6.033756E-10
-8.099900E-10 -1.079451E-09 -1.428627E-09 -1.878338E-09
-2.454132E-09 -3.187200E-09 -4.115422E-09 -5.284574E-09
    -6.749691E-09 -8.576622E-09 -1.084376E-08 -1.364400E-08
```

Appendix E Utility Programs

GEN DAMP

GEN_DAMP generates a damping file given the location of the damping layers (north, south, east, or west boundaries of the grid), the width of the damping layer, and the nondimensional damping strength at the end of the damping layer, μ_w . The damping values are initially set to zero over the entire grid. The program then calculates the spatial variation of the damping values over the width of the damping layers using a quadratic function, e.g.,

$$\mu_{nd}(x,y) = \left[\frac{x-x_0}{x_w-x_0}\right]^2 \mu_w$$

where x_0 and x_w are the coordinates of the beginning and end of the damping layer. The program is run interactively from an MS-DOS command prompt window. An example is as follows:

```
C:\bouss2d\bin\gen_damp
bathy  # name of input bathymetry file (.grd)
damp  # name of output damping file (.grd)
0  # width of damping layer - North (m) [0.0]
0  # non-dimensional damping strength (0-1) [0.0]
100  # width of damping layer - East (m) [0.0]
1  # non-dimensional damping strength (0-1) [0.0]
0  # width of damping layer - South (m) [0.0]
0  # non-dimensional damping strength (0-1) [0.0]
0  # width of damping layer - West (m) [0.0]
0  # non-dimensional damping strength (0-1) [0.0]
```

To effectively damp out waves at open boundaries, a damping layer half a wavelength wide with a damping strength of 1.0 should be used. The damping file is written out as an ASCII file in the grid file format described in Appendix D.

MAP_POROSITY

MAP_POROSITY creates a porosity grid file given the boundaries of porous regions within the computational domain as a set of discrete (x,y) points. The

Appendix E Utility Programs E1

porosity values are initially set to 1.0 over the entire grid. The program then uses the "Winding-Number" algorithm of Gordkin and Pulli (1984)¹ to set the porosity values within the porous region boundaries to values specified by the user. The (x,y) coordinates of the porous region boundaries are stored as two columns of data in an ASCII file. The program is run interactively from an MS-DOS command prompt window. An example is as follows:

```
C:\bouss2d\bin\map_porosity
bathy  # name of input bathymetry file (.grd)
porosity  # name of output porosity file (.grd)
2  # number of porous regions [1]
bw1.xy  # name of boundary file for porous region #1 [.xy]
0.4  # porosity (0-1) [0.4]
bw2.xy  # name of boundary file for porous region #2 [.xy]
0.4  # porosity (0-1) [0.4]
```

The porosity file is written out as an ASCII file in the grid file format described in Appendix D.

References cited in this appendix are listed in the References at the end of the main text.

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BOUSS-2D is a comprehensive numerical model for simulating the propagation and transformation of ocean waves in coastal									
regions and harbors. The model is based on depth-integrated Boussinesq-type mass and momentum equations for nonlinear-dispersive									
waves. The equations describe most of the wave transformation phenomena of interest in coastal regions and harbors including shoaling, refraction, diffraction, reflection, nonlinear wave-wave interactions, and wave breaking. This manual describes the theoretical									
background behind the model and the steps involved in setting up and running the model.									
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BOUSS-2D Wave Model in SMS: 2. Tutorial with Examples

by Zeki Demirbilek, Alan Zundel, and Okey Nwogu

PURPOSE: The purpose of this Coastal and Hydraulics Engineering Technical Note (CHETN) is to demonstrate the use of BOUSS-2D in three example applications. The BOUSS-2D is a Boussinesq wave model that is now part of the U.S. Army Corps of Engineers (USACE) Surface-Water Modeling System (SMS). Demirbilek et al. (2004) gives a detailed description of the SMS interface of BOUSS-2D. This second technical note in BOUSS-2D series is a step-by-step tutorial that shows the usage of the model through illustrative examples. The next CHETN in the series will describe the time-series and frequency-domain analysis utilities and techniques developed for post-processing BOUSS-2D model results. Details of the BOUSS-2D model theory, numerical implementation, and example applications are presented in a technical report (Nwogu and Demirbilek 2001).

BACKGROUND: As a phase-resolving nonlinear wave model, BOUSS-2D can be used in the modeling of various wave phenomena including shoaling, refraction, diffraction, full/partial reflection and transmission, bottom friction, nonlinear wave-wave interactions, wave breaking and dissipation, wave runup and overtopping of structures, wave-current interaction, and wave-induced currents. A comprehensive understanding of the BOUSS-2D interface in SMS is necessary for maximizing the benefits of this tutorial. This CHETN will also prepare users for the third follow-up note in this series about analysis utilities developed for BOUSS-2D model.

Wave estimates in navigation design, maintenance and operation studies, channel sedimentation, inlets, and harbors are affected by the seabed topography, tidal currents and coastal structures present in the areas of interest. These features cause temporal and spatial changes in the wave field that can be estimated using an advanced nearshore wave propagation model such as the BOUSS-2D. The model employs a time-domain solution of fully nonlinear Boussinesq-type equations, valid from deep to shallow water, representing the depth-integrated equations of conservation of mass and momentum for waves propagating in water of variable depth. Input waves to BOUSS-2D may be periodic (regular) or nonperiodic (irregular), and both unidirectional or multidirectional sea states may be simulated.

The governing equations in BOUSS-2D are solved in the time domain with a finite-difference method, from which water-surface elevation and horizontal velocities are calculated at the grid nodes in a staggered manner. Waves propagating out of the computational domain are absorbed in damping layers placed around the perimeter of the domain. Damping and porosity layers can also be used to simulate the reflection and transmission characteristics of jetties, breakwaters, and other structures existing in the modeling domain. These and other details about BOUSS-2D model are provided in the model report, containing six examples that illustrate model's versatility and features (Nwogu and Demirbilek 2001).

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The SI engineering units are used in BOUSS-2D calculations. Data in English units can be imported into the SMS interface and converted to metric. For example, bathymetric data in latitude/longitude can be converted in the model interface to UTM or State Plane coordinates. Likewise, model results can be presented in English units using conversion tools and data calculator features available in SMS. The interface of BOUSS-2D in SMS (Zundel et al. 1998; and Zundel 2005) facilitates grid generation and specification of model parameters. Model input and output may be pre- and post-processed in different formats, using two- and three-dimensional (2- and 3-D) display and visualization options and a variety of animation types (see Demirbilek et al. 2004). The bathymetry, wave data, and model parameters used in BOUSS-2D simulations are formatted into specific file formats in the SMS interface. The users must assemble input bathymetry and wave data for a BOUSS-2D simulation from appropriate data sources. Data sources are accessible from within SMS for bathymetry and coastlines, and other commercial databases that may also be used to assemble the requisite input for BOUSS-2D model

The emphasis of this CHETN is to provide description of a few typical examples for BOUSS-2D simulations. The examples should be helpful to users in practical applications. In the first example, step-by-step instructions are described in a complete BOUSS-2D simulation for prediction of the wave climate in Barbers Point Harbor, HI. In this case, details of each step are presented for the understanding of the modeling process used in BOUSS-2D. In the last two examples, the model's features and capabilities for wave-structure interaction problems are demonstrated. The second example shows application of the model to a jettied inlet, illustrating the use of porosity layers around jetties or breakwaters. The third example demonstrates the use of a simplified 1-D version of the Boussinesq model to estimate wave runup and overtopping of idealized sloping structures.

EXAMPLE 1 – BARBERS POINT HARBOR, HI:

Images: It is often useful to have background images to help orient numerical grids in a simulation, and to place coastlines and structures with precision that exist in the modeling region. These images may be digital bathymetry charts or aerial photographs. In this example, two images were downloaded from the TerraServer site http://terraserver.homeadvisor.msn.com. These digital bathymetric charts cover a small portion of coast on southwest corner of the island of Oahu, HI. Use *File/Open* and select the file topo1.jpg to read in the first image. The Internet-based resource also provides a world file to geo-reference this image. Should SMS ask if image pyramids are desired, select the toggle to not ask this question again and click **Yes**. Repeat the file opening procedure for file topo2.jpg. SMS will piece together these two images (Figure 1).

After reading these images into SMS, tell it what coordinate system the data are referenced to. The coordinate system is dependent on the data source. For the TerraServer site, all world files register the images to UTM coordinates in NAD83. To pass this information to SMS, select *Edit/Current Coordinates*, and specify UTM NAD 83 (US), select the horizontal and vertical units as "meters" and the UTM Zone as Zone 4. Images may be used to define land boundaries of modeling domain and structures.

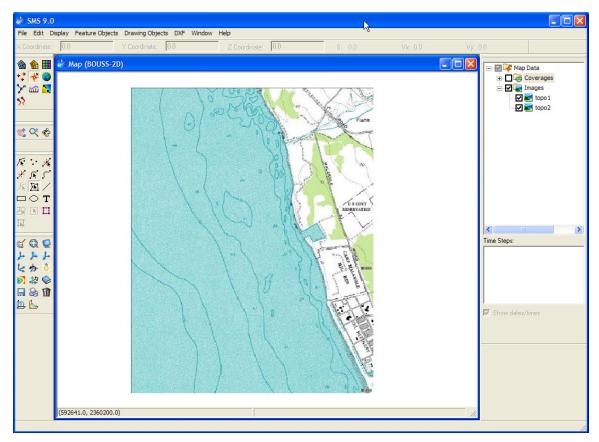


Figure 1. Images of simulation region

Bathymetry: BOUSS-2D needs bathymetric data to define the shape of the seafloor. For this example, a local survey was performed and bathymetry was available in ASCII files. To bring the survey into SMS, select *File/Open* and select the file BP_bathy_filtered.pts. This file includes depth values in the Barbers Point Harbor and the immediate coastal region outside the harbor. These data are referenced to UTM Zone 4. The survey points displayed over the background image are shown in Figure 2. SMS triangulates the points to create a piecewise linear surface covering the entire region. The outer lines around the points depict the extent of this surface. It should be noted that regions of coastal land are covered by this surface, but not represented since all of the survey data points were in the water. The triangles covering the land must therefore be deleted in order to define which areas are land and which are water, otherwise SMS will interpolate between the harbor and coast without realizing there is land between them.

Coastlines: A coastline can be used to define the interface between land and water. For this example, the coastline for the island of Oahu has been extracted. To see this region, select *File/Open* and choose the file BP_coast.cst. The coastline will be read in and displayed as shown in Figure 3.

There is more coastline here than is needed, which includes many other harbors, land features, and islands unrelated to Barbers Point Harbor. The user may use the following steps to trim the coastline to the area involved:

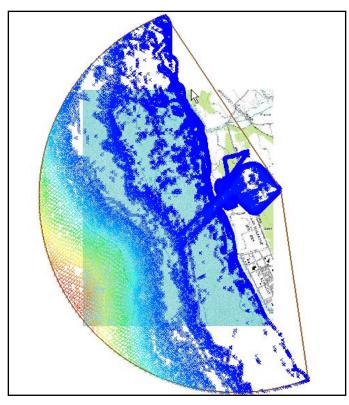


Figure 2. Bathymetry points for sample problem

- a. Zoom into the area being modeled.
- b. In the Map module **, select the Create Arc tool .
- c. Click on the coastline just north of the data (P1 in Figure 4), then click inland (P2) and then on the coastline east of the simulation area (P3).
- d. Switch to the Select Arc tool and select the coastline away from area of interest and hit the **Delete** key to eliminate this arc (Arc to delete in Figure 4).
- e. Frame the display and drag a box around the island arcs and delete them. (This is easily done by dragging a box around the islands on the north side of Oahu and deleting them, and then dragging a box around the islands on the east side.)
- f. Build a polygon to represent the land around Barbers Point by selecting Feature Objects/Build Polygons.

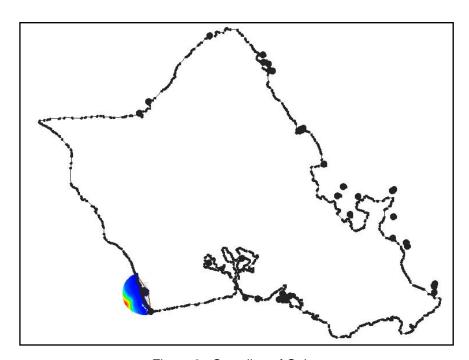


Figure 3. Coastline of Oahu

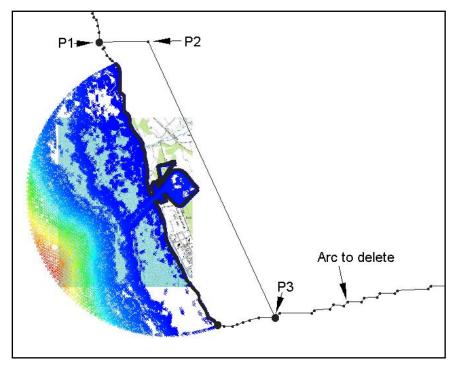


Figure 4. Bisecting arc separates areas around simulation from rest of island coastline

- g. Select the Select Polygon tool , and select the land polygon.
- *h.* Choose *Feature Objects/Select/Delete Data* ... This brings up the dialog shown in Figure 5. Set the options to delete triangles inside the polygon and click **OK**.

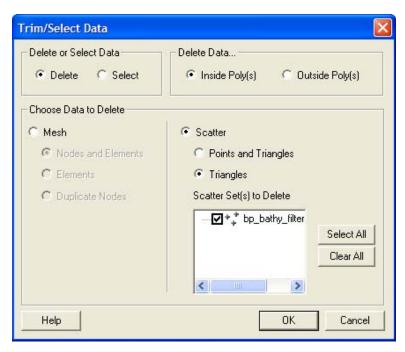


Figure 5. Trim/Select Data options

There is now a surface that represents the seabed around the region of Barbers Point Harbor in Hawaii. The next step is to create a computational grid for BOUSS-2D.

Create Grid: The computational domain of BOUSS-2D is a Cartesian grid that can be defined with three clicks. In this example, instructions are provided to ensure consistency. To create the grid, follow these steps:

a. Zoom into harbor as shown in Figure 6.

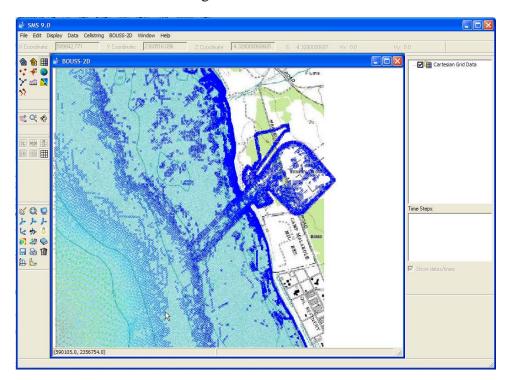


Figure 6. Zoomed view displaying area for creating computational grid

- b. Make sure the 2D Cartesian Grid Module is the current module and that BOUSS-2D is the active model. User should see a BOUSS-2D menu at the top menu bar in SMS. If this is not the case, select Data/Switch Current Model and select BOUSS-2D.
- c. Select the *Create Grid tool* Click near the point P1 (Figure 7). An exact location of points can be specified later. The coordinates of the cursor are displayed on the lower left corner of the window.
- d. Move the mouse toward shore and inland. At the bottom of the window, the size of resulting grid is displayed. Click on point P2 (Figure 7), approximately 2,500 m from the first point.
- e. Move the mouse up to include harbor approximately 2,000 m from second point and click in the area of point P3 (Figure 7).

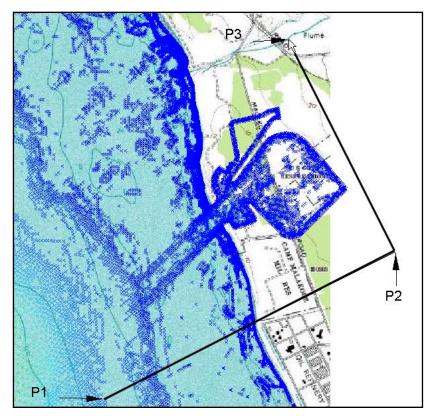


Figure 7. First and second click point when defining grid

f. After the third click, SMS will display a dialog to create the grid (Figure 8). For consistency in this exercise, modify the grid parameters in this dialog to match the values in the dialog as shown. The cell sizes are dependent on the wavelength. The Courant number that controls the stability of numerical solution in BOUSS-2D is used to determine time-step from the cell size. Note that the cell size is generally expressed as a fraction of the wavelength. Care should be exercised in selecting cell sizes. The model report (Nwogu and Demirbilek 2001) describes how to determine cell size based on wavelength. Smaller cell sizes may guarantee stability of runs, but require excessive computing time. Larger cell sizes will cut down the runtime, but may cause model instability. It may be necessary to also check sensitivity of model results to cell sizes using more than one grid.

With the previous issues in mind, users should determine the most appropriate grid resolution (cell size) in an application based on consideration of both the available resources and model computational requirements. The cell size of 10 m is used in this example. In the *Depth Options*, click the button labeled **elevation** (**Z**). This will bring up the *Interpolation* dialog (Figure 9). Set the extrapolation elevation on the left side to 1 m that will assure the land will be treated as land. This step would not be required if survey data included points on the shore with positive elevations. Click the **OK** buttons on both the dialogs to create the grid.

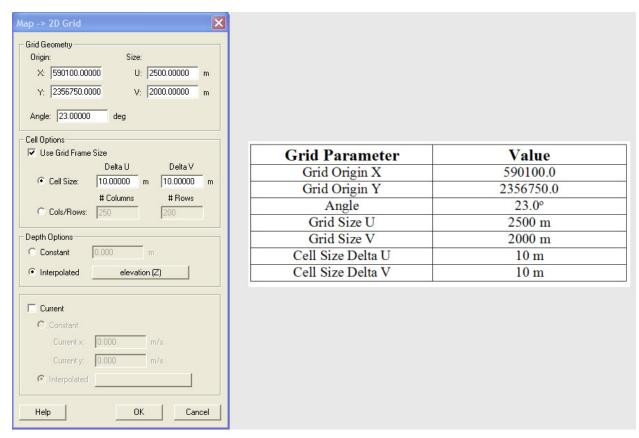


Figure 8. Parameters to create grid

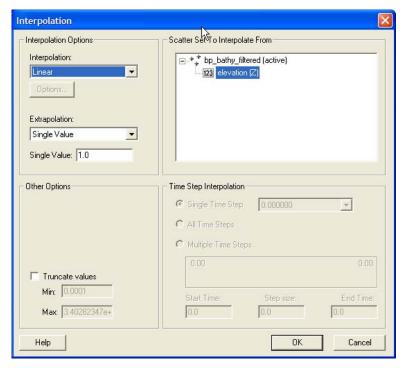


Figure 9. Interpolation options to assign bathymetry values

Figure 10 shows the resulting grid boundary. The computational (ocean) area is outlined in the darker colors. The area on the right (land) is inactive, and model calculations are not performed in the land regions.

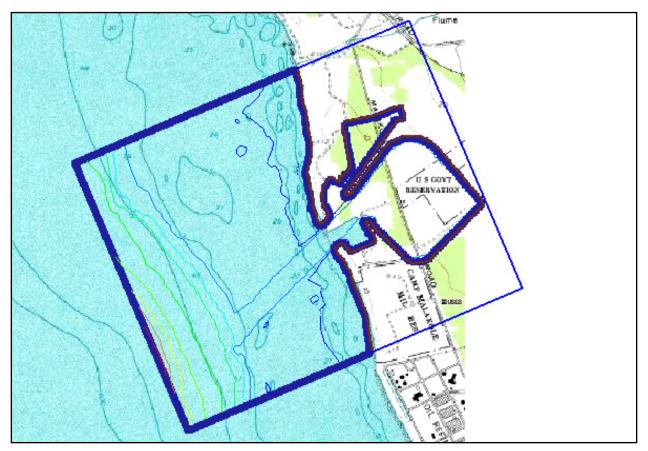


Figure 10. Resulting grid

Define Wave Maker: The BOUSS-2D is a numerical wave tank, and the layout of its modeling domain is similar to the setup of a laboratory (physical model) study. The BOUSS-2D wave maker must be positioned along a straight line that can be referred to here as a "cell string" in the SMS terminology, and at a desired location where depth is ideally constant. The previously defined grid creation process automatically generates cell strings along the edges of the computational area. Cell strings can also be created manually to specify the location of structures, wave makers, and areas where damping and/or porosity layers may be necessary. To define a wave maker, follow these steps:

- a. Select the *Select Cell String* tool **...**.
- b. Select the cell string (in red) on the left side of the grid as shown in Figure 11, where wave maker is to be situated.

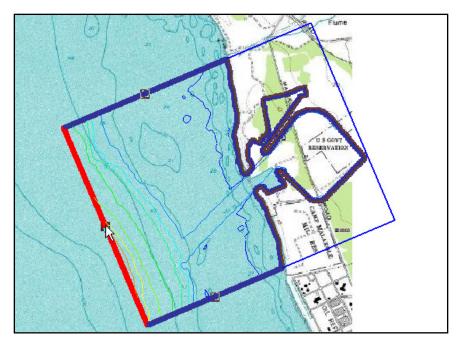


Figure 11. Wave maker cell string selected

- c. Select BOUSS-2D/Assign BC command. Select the Wave Maker radio button and click on the **Options** button. This brings up the BOUSS-2D Wave Generator Properties dialog. On the left side of this dialog select the type of wave to simulate, i.e., irregular unidirectional waves. Select the defaults to synthesize the time series and generate them from parameters. Specify the series duration as 1,500.0 sec in this example. On the right side, select the spectra type to be JONSWAP, and the option to specify significant wave height and peak period values, H_s and T_p. Enter values of significant wave height and peak period as 3.0 m and 15.0 sec., respectively. Click **OK** to close both the dialogs. For further details on wave spectra types and associated spectral parameters, users should consult Demirbilek et al. (2004) and Nwogu and Demirbilek (2001).
- d. As SMS generates the wave maker, it may find that the offshore edge of the grid is not of constant depth, and warn the user. At this point the user is given the option of extending the grid to a constant depth to improve model stability. Click the **Yes** button to extend the grid in order to complete proper definition of the wave maker location.

Define Damping Layers: Damping layers may be specified along boundaries of the computation zone where waves need be absorbed. Damping layers prevent waves from reflecting back into the computational area. This may be necessary since reflected waves will affect the incident waves. In this example, damping layers will be assigned to both lateral boundaries of the modeling domain that will absorb waves leaving the domain. To do this:

- a. Select the cell strings along the open sides of the grid between deep water and the coastline. To select two cell strings, click on the first and hold the **SHIFT** key to click on the second cell string.
- b. Select BOUSS-2D/Assign BC... and select Damping.

c. Enter values of 40 m for the width of damping layers and 1.0 for the damping coefficient and select **OK**. The width value for the damping depends on several factors including wave type and grid resolution. Consult Demirbilek et al. (2004) and Nwogu and Demirbilek (2001) for details.

In applications where the depth transition from water to land is not gradual, excessive reflection would occur as the model overpredicts reflection from the coast. To prevent this, place a damping layer along the coastline. This coastline damping-layer may be defined as:

- a. Select the cell string along the coastline.
- b. Select BOUSS-2D/Assign BC... and select Damping.
- c. Enter values for width and damping coefficients of 20 m and 0.5, respectively, and select **OK**. These values allow for partial reflection.

Specify Other Model Parameters: The next step in preparing a simulation is to specify other model input parameters. Select *BOUSS-2D/Model Control* to specify *Project Title* as "Barbers Point Sample Run." In the *Input Data Sets*, select **Use Cellstrings** for damping. For *Porosity and Current*, choose **None**. For *Time Control*, enter 1,500 sec for duration of the run, and 0.2 sec for the time-step. For *Animation Output*, check *Output WSE*, *Output Velocity* and *Override Defaults* toggles. Enter 1,425.0 for the beginning time; 1,500.0 for the ending time; and 1.0 sec for the output interval to save an animation output for approximately the last five waves. Select the **OK** button to close the dialog box.

Save and Run Simulation: The final step before running a simulation is to save the BOUSS-2D files. Select $File/Save\ New\ Project$ and enter **BarbersPoint_Tutorial** for project name, and click **OK**. The simulation may now be launched by selecting $BOUSS-2D/Run\ Bouss$. A message will be displayed for the default location of the model executable (Bouss2d.exe). Click on the folder icon to select the location of "Bouss2d.exe" file, and click on the **Run** button. SMS now launches BOUSS-2D. This simulation takes approximately 1 hr to run on a Pentium 4 processor (3 GHz clock speed) with a 0.2 sec time-step. The model run time would increase to nearly 3 hr for a grid using $5-\times 5$ -m cells, and the run time would reduce to below 20 min for a grid with $20-\times 20$ -m cells.

Visualize Simulation Results: The model will create five solution files that include spatially varying results at the grid nodes. Three of these are steady state data sets that include the results for mean wave height, mean current direction, and mean water level. The other two are temporally varying results, output at user-specified intervals. These include computed water levels and currents (u and v). BOUSS-2D saves these results in the independent files named BarbersPt_hs.grd, BarbersPt_mean_uv.grd, BarbersPt_mwl.grd, BarbersPt.eta and BarbersPt.uv. The model can also write all of these in one binary metafile named BarbersPt.h5 in HDF5 format. When the model run is completed, the user can select a toggle to read the type of solution files for SMS to display. Refer to Demirbilek et al. (2004) and the SMS users manual and tutorials for guidance on how to visualize the model output files.

After the model run is complete, make sure the toggle to read the solutions is checked and click the **Exit** button. To display a functional surface of the water surface, select the *Display/Display Options* command and turn off the cells toggles (both water and land) and turn on the *Functional Surface* toggle. Click on the **Options** button right below the toggle to bring up the *Function Surface Options* dialog. In the upper left corner select the *User defined data set* option, click the **Select** button and choose *WSE Animation* from the list of data sets. Next, click the **Select** button in the *Select Data Set* dialog. You can use the *Choose Color* button to select a color for the functional surface, followed by clicking **OK** to close the *Functional Surface Options* dialog. Back in the *Display Options* dialog, choose the *General* tab and set the *Z magnification* to 20.0. Next, select the *Contours Options* tab and change the *Contour Method* to *Color Fill*, and click **OK**.

To give the surface some feature, select *Display/Lighting Options* and select *Use light source*. Turn on the *Smooth features*, click on the upper right side of the sphere, and then click **OK**. Finally, select the *Depth* data set for contouring the bottom of ocean, and select *Display/View/View Angle* and enter values of 40 and 25 for the bearing and dip. Figure 12 shows this functional surface of the water surface overlaying the bathymetric surface.

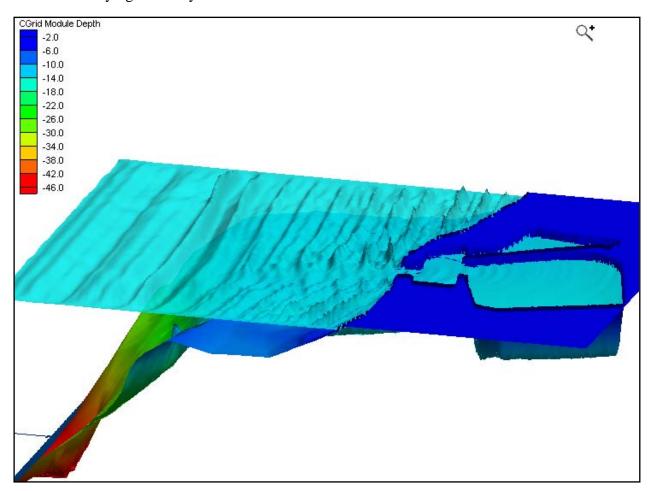


Figure 12. Functional surface of water levels over bathymetry (magnified 20x)

EXAMPLE 2 – MODELING WAVES AT A JETTIED INLET:

All the necessary steps have been shown in Example 1 for constructing a complete BOUSS-2D simulation. In this example, the only discussion will be the creation of porosity layers that were not used in the first example. For illustration purposes, porosity layers will be placed around one of the jetties in this example. All other features to be considered in this application are the same as in Example 1, and will therefore be omitted. To start a new project from an existing SMS application, select the **File|Delete All** command to clear out the Barbers Point simulation. Now select the **File|Open** command and choose the file IdealInlet.par to open the existing simulation of an ideal inlet that has a jetty on either side of the inlet. The modeling domain is shown in Figure 13. This grid was generated following steps described in Example 1.

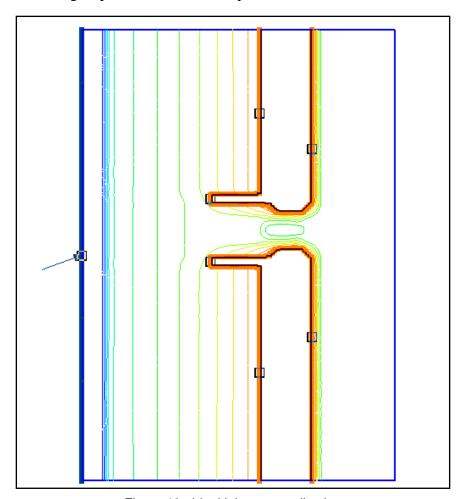


Figure 13. Ideal inlet test application

The existing grid was set up with the damping layers placed along the coastlines and around both jetties. To be consistent, damping layers should be used for coastlines and porosity layers for breakwaters and jetties. Porosity layers will be placed around the south jetty for modeling the interaction of waves with a porous structure. The following steps can be used:

a. Select the cell string that goes along the south jetty.

- b. Select the **BOUSS-2D**|**Assign BC** command. Choose the *Porosity* radio button and enter a value of 20 m for the width and 0.5 for the porosity value. Click the **OK** button. For details on how to select appropriate values for these parameters, users should refer to Demirbilek et al. (2004) and Nwogu and Demirbilek (2001).
- c. Select the *BOUSS-2D/Model Control* command. In the upper right corner, set the *Porosity* choice to **Use Cellstrings**. Enter a value for the characteristic stone size on the right side of the dialog as 0.75 m. Click the **OK** button to exit the *Model Control* dialog.
- d. Save the simulation with the **File|Save BOUSS-2D** command. When asked, tell SMS to replace the damping function. This simulation is now ready to be run. Follow the steps given in Example 1.

Figure 14 shows the waves around the porous jetty (in the foreground) as compared to the extra bending of the waves on the nonporous jetty.

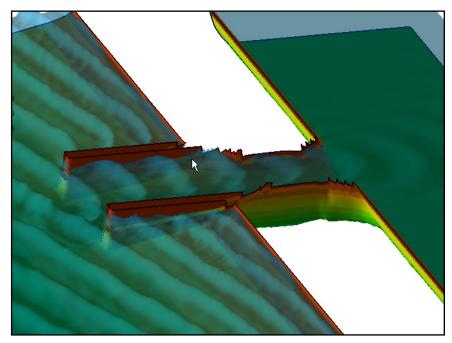


Figure 14. Waves around porous jetty

EXAMPLE 3 -- WAVE RUNUP AND OVERTOPPING OF BREAKWATER:

BOUSS-2D can simulate the wetting and drying of arbitrary 2-D coastal topographies. A simplified version of the 1-D model (BOUSS-1D) has been developed to predict the runup and overtopping of impermeable coastal structures. In this example, the usage of BOUSS-1D for prediction of wave runup on a sloping structure will be demonstrated. The model supports any geometrical profile, but for design purposes, the runup and overtopping calculator in SMS automatically creates a profile of the form shown in Figure 15. This geometric template is similar to the physical modeling work done by Saville (Saville 1955).

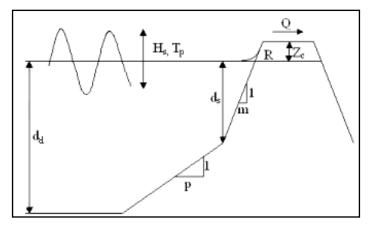


Figure 15. Profile shape generated by SMS for BOUSS-1D

The user enters a wave height and period along with the geometrical description of the structure. These are the maximum depth (d_d) , toe depth (d_s) , crest elevation of the structure (z_c) , structure slope (m) and a beach slope (p). Described here are the steps in applying BOUSS-1D to the estimation of maximum wave runup situations.

The runup and overtopping calculator is accessed by selecting the **BOUSS-2D**|Calculators command and choosing the *ID Runup and Overtopping* tab (Figure 16).

The BOUSS-1D utility tries to predict wave-surface elevation time-history, from which estimates of wave runup and overtopping are computed. For regular incident waves, the estimated runup is the maximum runup, whereas for irregular waves, it is the $R_{2\%}$. The overtopping refers to the volume of fluid passing over the crest width of the structure, which determines the amount of fluid arriving on the backside of the structure.

As an example, if the user enters the values shown in Figure 16, and click on the **Calculate** button, SMS will create the input file for the simulation and bring up a prompt asking for the version of Boussinesq model to run. Select *BOUSS-1D* to run and click **OK** button. At this point SMS launches BOUSS-1D and displays the progress. This may take 10 to 20 sec to run. The model wrapper indicates the model run is complete and the user selects the **Exit** button. The runup and overtopping values appear in the bottom section of the calculator.

It should be pointed out that the Boussinesq equations on which the model is based implicitly assume that the seabed or structure slope is mild, relative to the characteristic wavelength. When SMS constructs the input file, the wavelength at the toe is compared to the wetted length of the structure. If the mild slope assumption is violated (i.e., a characteristic wavelength cannot fit on the structure, SMS modifies the slope term "m" to be a maximum value computed as the wavelength at the toe of the structure divided by 2 times the depth at the toe of the structure. In this case, a message will be echoed to the screen indicating that the mild slope assumption was violated and the predicted runup value may be not reliable or less accurate. If the model fails, it returns a value of 0.0 for runup. For the mild slope structures (1:6 and 1:10 slopes) tested in the Saville experiments (Saville 1955), the BOUSS-1D model predicted values of runup are generally within 20 percent of the physical model data. The prediction of runup can be improved by calibrating the model with the experimental data.

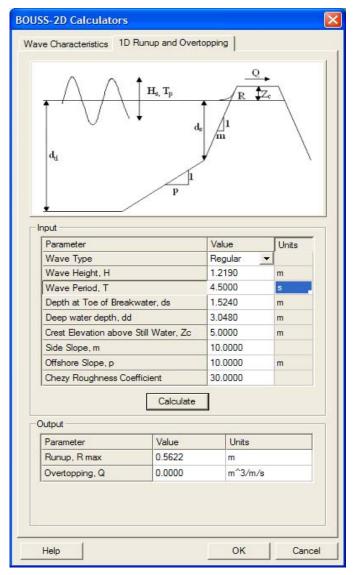


Figure 16. Wave Runup and Overtopping calculator

SUMMARY: This note is applicable to the Version 1.0 of BOUSS-2D. Three examples have been used in this CHETN to illustrate the steps involved in typical application of BOUSS-2D. These involve modeling waves in a harbor, a jettied inlet and the prediction of wave runup and overtopping of a sloping coastal structure. Coastal projects may require simulation of many wave conditions and different grids representing different structures or other modifications as required in the study site. The users can explore a number of features and capabilities of BOUSS-2D in such cases. Specific guidance is provided to the users in this CHETN to ensure a solid understanding of the methodology when applying BOUSS-2D model to different engineering problems. With increasing use of BOUSS-2D in engineering projects by the community, it is expected that both the model and its interface will evolve, and the Version 1.0 of BOUSS-2D model and its SMS interface will continue to undergo future revisions. Feedback and suggestions are welcome from users about design, implementation, and usage of the present and future versions of BOUSS-2D model.

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